

Run Like a Neural Network, Explain Like k-Nearest Neighbor

Xiaomeng Ye¹, David Leake², Yu Wang² and David Crandall²

¹Berry College

²Indiana University Bloomington

xye@berry.edu, {leake,yw173,djcran}@iu.edu

Abstract

Deep neural networks have achieved remarkable performance across a variety of applications. However, their decision-making processes are opaque. In contrast, k-nearest neighbor (k-NN) provides interpretable predictions by relying on similar cases, but it lacks important capabilities of neural networks. The *neural network k-nearest neighbor* (NN-kNN) model is designed to bridge this gap, combining the benefits of neural networks with the instance-based interpretability of k-NN. However, the initial formulation of NN-kNN had limitations including scalability issues, reliance on surface-level features, and an excessive number of parameters. This paper improves NN-kNN by enhancing its scalability, parameter efficiency, ease of integration with feature extractors, and training simplicity. An evaluation of the revised architecture for image and language classification tasks illustrates its promise as a flexible and interpretable method.

1 Introduction

The importance of explaining AI system behavior is widely acknowledged. The dominance of neural network models has prompted numerous efforts to develop explanation components that provide post-hoc explanations of neural systems [Guidotti *et al.*, 2018; Adadi and Berrada, 2018]. However, Rudin *et al.* [2022] advocate a different path: developing inherently interpretable models rather than relying on post-hoc explanations for black-box models. They argue that post-hoc explanations often fail to accurately reflect the reasoning process of black-box models, potentially misleading users. In contrast, inherently interpretable models enhance trust and can expose potential flaws in the data, which is particularly advantageous in high-stakes applications.

The k-nearest neighbor (k-NN) algorithm is a classic interpretable algorithm. It predicts the label of a query by analyzing the k most similar instances from previously observed data and combining their results, generally by straightforward methods such as averaging or majority vote [Cover and Hart, 1967]. The k-NN decision-making process, directly influenced by neighboring data points, enables intuitive, instance-based explanations. Despite its simplicity, k-

NN has demonstrated competitive performance across diverse datasets, often achieving accuracy comparable to more complex machine learning models [Rudin, 2019]. However, its effectiveness depends heavily on factors such as feature selection, distance measures, instance weighting, and feature weighting. This poses challenges when fine-tuning the model for more complex datasets [Kulis, 2013; Park *et al.*, 2004; Weinberger and Saul, 2009; Bellet *et al.*, 2015]. More recent variations of k-NN, such as Large Margin Nearest Neighbor (LMNN) [Weinberger and Saul, 2009] and Neighborhood Components Analysis (NCA) [Goldberger *et al.*, 2004], partially address these challenges by learning transformations of the feature space to improve classification accuracy.

However, k-NN struggles with high-dimensional or large-scale data due to the cost of exhaustive comparisons, difficulty in feature selection, and the curse of dimensionality. Various efforts tackle these challenges [Jalali and Leake, 2018; Johnson *et al.*, 2019]. In contrast, neural networks excel at capturing abstract representations, hidden patterns, and the relative importance of features in high-dimensional spaces. They also leverage tensor computations and parallel computing to handle large datasets. The contrasting strengths and weaknesses of k-NN and network models make it appealing to develop hybrids harnessing the strengths and alleviating the weaknesses of each. For example, Li *et al.* [2018] propose a model in which a prototype layer stores embeddings of learned prototypes and uses them in classification. Because the network relies on the prototype layer for classification, its decision can be interpreted in terms of activated prototypes.

Inspired by Li *et al.* [2018], Ye *et al.* [2024] introduced *neural network based k-nearest neighbor* (NN-kNN), a hybrid model aiming to provide both the interpretability of k-NN and the learning capabilities of neural networks. The NN-kNN architecture reimagines the k-NN process within a neural network framework, integrating feature extraction, similarity assessment, and prediction into a cohesive, end-to-end trainable model. This design enables NN-kNN to simultaneously learn feature importance [Wettschereck *et al.*, 1997], case weights [Bicego and Loog, 2016], and distance metrics, enhancing its adaptability and performance.

The initial NN-kNN provided multiple benefits, but it also had limitations: (1) As datasets grow in size and complexity—as for natural images or text embeddings—the computational cost of comparing a query to every stored case

becomes prohibitive,

(2) Its reliance on raw features limits its ability to capture hidden patterns effectively, and (3) Its feature weighting scheme either assigned identical weightings to all cases, or assigned unique weightings to each case. This method could underfit by neglecting local patterns or overfit by assigning weights too specifically to individual instances.

This paper presents work on extending NN-kNN to address these limitations. Our key contributions include:

1. **Scalability by Case Sampling.** We introduce a sampling mechanism that selects a subset of cases to use during training and inference, significantly reducing computational cost.
2. **Feature Extraction for High-Dimensional Data.** We integrate a feature extraction layer in NN-kNN, which can be either pretrained or jointly trained end-to-end with NN-kNN. This enables NN-kNN to effectively process high-dimensional data, expanding its applicability to domains like image classification and NLP.
3. **Global-local (“Glocal”) Feature Weighting Scheme.** We present a feature weighting mechanism that combines global feature weights with case-specific coefficients to compute adaptive weights for each case. This reduces the number of parameters while maintaining flexibility.
4. **Activation Function for Differentiable k-NN.** We created a custom differentiable activation function for k-NN. Cases within a chosen proximity activate, while other cases have near-zero activations.
5. **Evaluation on Image and Language Benchmarks.** To validate the effectiveness of our extended NN-kNN, we conduct experiments on natural image classification and language classification. NN-kNN both predicts and explains its predictions using the top activated cases.

Our results support that the extended NN-kNN retains the intuitive, case-driven explanations of traditional k-NN while addressing critical previous limitations. By bridging the gap between classical k-NN and neural networks and integrating with state-of-the-art neural feature extractors, NN-kNN provides functionality for interpretable and scalable systems.

2 Related Work: Metric Learning and the Original NN-kNN Model

A simple k-NN approach assumes that all features contribute equally to the distance calculation and that all cases are equally important in the domain space. Wettschereck et al. [1997] present a more general distance calculation, and extensive research on distance metric learning has produced numerous k-NN variants [Bellet et al., 2015; Kulis, 2013; Park et al., 2004; Bicego and Loog, 2016]. Among these, Neighborhood Components Analysis (NCA) [Goldberger et al., 2004] and Large Margin Nearest Neighbor (LMNN) [Weinberger and Saul, 2009] are particularly notable for their ability to learn linear transformations of the feature space, enhancing classification accuracy.

The neural network based k-nearest neighbor (NN-kNN) model [Ye et al., 2024] reimagines the k-NN process within a neural network architecture. Its architecture computes feature distances, case activations, and class activations in a sequential manner. This design enables NN-kNN to learn feature importance, case weights, and distance metrics directly from data in an end-to-end training process, while remaining interpretable as the intuitive, instance-based reasoning of traditional k-NN. The model has shown competitive performance with neural networks in basic classification and regression tasks. However, the original NN-kNN model faced several limitations, for scalability to large datasets, handling high-dimensional data, and restricted feature-weighting options. This paper presents an extended model addressing these issues. To differentiate the old and new models, we will refer to the original as NN-kNN_O.

3 Design of the Extended NN-kNN

We extend NN-kNN_O for large-scale and high-dimensional datasets. Each case c is associated with a default activation strength $bias_c$ (indicating the range of queries that activate the case), a *case_weight* (indicating the extent to which case activates a class) and a one-hot encoded class label. Figure 1 illustrates the overall workflow of NN-kNN, as explained below. Only in step 3 is the process identical to NN-kNN_O.

1. **Sampling Cases for Comparison:** A query q is compared with a subset of cases from each class.
2. **Extracting Features:** The feature extraction layer maps input x (a query or a case) to a d -dimensional vector, $f(x) = \langle x_1, x_2, \dots, x_d \rangle$. For example, ResNet can be used for image data [He et al., 2016], and doc2vec for text data [Le and Mikolov, 2014].
3. **Calculating Feature Distances:** The feature distance layer δ measures distance between each corresponding feature j of the query q and the case c as $\delta_j(q_j, c_j)$ (abbreviated as δ_j). In this work, we use Euclidean distance.
4. **Summing Weighted Feature Distances:** Each feature distance δ_j is scaled based on its importance cw_j (see Section 3.1). The weighted distances are summed to compute the overall distance between q and c .
5. **Activating the Case c :** Case c ’s activation is calculated based on a function of the difference between $bias_c$ and the distance from q (see Section 3.2).
6. **Activating the Class:** The case activation is multiplied by the case weight and its one-hot encoded label to contribute to the class activation. The sum of class activations is calculated for all cases, and the class with the maximum activation is chosen as the prediction.

3.1 Global-Local Feature Weighting

In NN-kNN_O, all cases either share a single global feature weighting or each has an individual feature weighting. The later approach tends to perform better because the model can learn to adjust to local landscapes in the task domain [Ricci

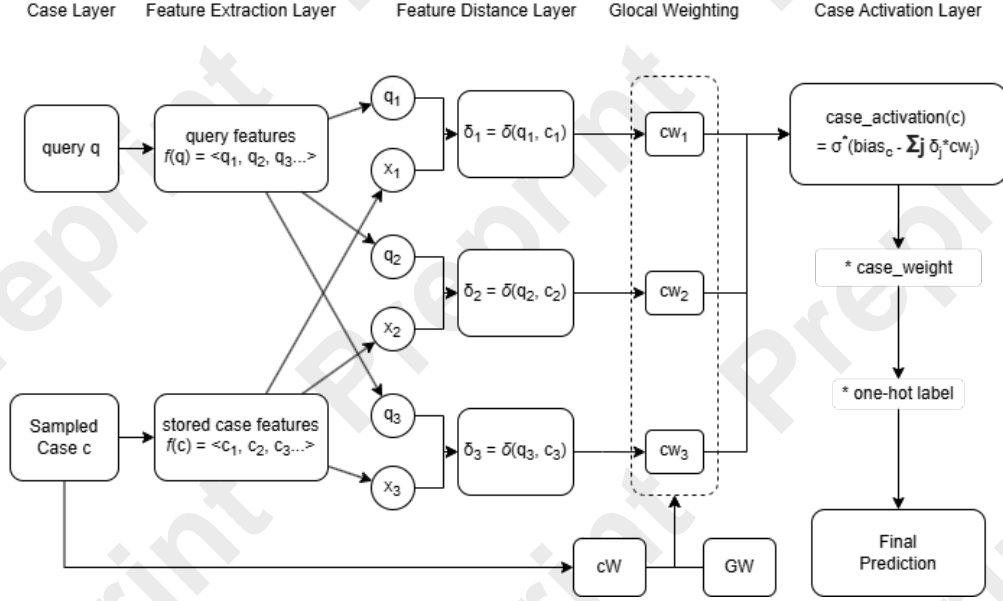


Figure 1: The Extended NN-kNN.

and Avesani, 1995; An *et al.*, 2018], but at the cost of many parameters to learn.

We introduce a global-local (glocal) feature weighting mechanism that bridges the gap between global and individualized weightings. The glocal approach enables tuning the amount of locality in weightings; from global to completely local. This flexibility enables balancing trade-offs in accuracy, storage, and weight learning costs.

We consider cases characterized by vectors of scalar features within a feature space of dimension d . This scheme uses a shared set of w global feature weights $GW = \{GW_1, GW_2, \dots, GW_w\}$ where each set $GW_i = \{w_{i1}, w_{i2}, \dots, w_{id}\}$ is a vector of length d . The weight w_{ij} represents the importance of feature j according to the global weighting GW_i . Each case c is associated with its own set of learnable coefficients $cW = \{cW_1, cW_2, \dots, cW_w\}$. Intuitively, cW_i quantifies how strongly case c is influenced by the global weighting GW_i .

The feature weights cw (different from cW) for a specific case c are calculated as the dot product of the coefficients cW and the global feature weights GW .

Testbed System Implementation Details

In the testbed system used for our experiments,

$$\begin{aligned} cw &= cW \cdot \text{leakyReLU}(GW) \\ &= \{cW_1 \times w_{1j} + cW_2 \times w_{2j} + \dots + cW_w \times w_{wj}\}_{j=1}^d \end{aligned}$$

This equation computes the feature weights cw of shape $1 \times d$ by the dot product of the case-specific coefficients cW ($1 \times w$) and the global weights GW ($w \times d$). A leakyReLU is applied here to ensure that all feature weightings in cw stay positive or close to 0. This design maintains the k-NN property that feature differences monotonically increase case distances. If there is a single global feature weight ($w = 1$),

feature weights are initially set to $w_{1j} = 1$ for every j , ensuring equal importance prior to training. If there are more global feature weights ($w \neq 1$), the weights w_{ij} are randomly initialized within $[0, 1]$.

When $d \gg w$, this design significantly reduces the parameter count for each case from d to w , enhancing computational efficiency while preserving the ability to capture local characteristics of the case space.

3.2 Case Activation Function

Traditionally, k-NN uses the parameter k to specify the number of neighbors to consider. NN-kNN uses a case activation function to distinguish between relevant and irrelevant cases. Let each case's $bias_c$ be initialized as B , the initial range of activation. NN-kNN uses a special scaled sigmoid function as the case activation function,

$$\text{case_activation}(c) = \sigma^*(bias_c - \sum_j (\delta_j cw_j)) \quad (1)$$

$$\sigma^*(a) = \sigma\left(\frac{8}{B} \cdot a - 4\right), \quad (2)$$

where $\sigma(a)$ is the standard sigmoid function,

$$\sigma(a) = \frac{1}{1 + e^{-a}}.$$

The scaled sigmoid function $\sigma^*(a)$ maps the raw case activation values from $[-\infty \dots bias_c]$ to the range $[0, 1]$. Cases identical to the query achieve the highest activation because $\sum_j (\delta_j cw_j) = 0$, resulting in $\sigma^*(bias_c) \simeq \sigma^*(B) \simeq 1$. Conversely, cases with distances exceeding $bias_c$ yield low activations, as $a < 0$ and $\sigma^*(a) < \sigma^*(-4) \simeq 0$. Without scaling, the raw activation may over-saturate a sigmoid function with its gradient plateaued to 0, making the training process difficult.

This activation function offers significant advantages over the traditional parameter k for the following reasons:

1. **Consistency:** B provides more consistent retrieval than k . Simply selecting the top k nearest neighbors disregards the relative distances of these neighbors to the query (distance-weighting can be applied but does not truly address this). For example, if the query is far from training cases, then selecting its top k nearest neighbors may retrieve cases far away from the query, while selecting cases within range B will only retrieve cases nearby.
2. **Case-Specific Customization:** $bias_c$ is individually tailored to each case c . A case with a high $bias_c$ indicates a larger radius of activation, or the ability to activate for a wider range of queries.
3. **Trainability:** Unlike a fixed parameter k , $bias_c$ can be trained to optimize the performance of the model.

Testbed System Implementation Details

In our experiments, we initialize $bias_c = B$ as the average unweighted distance of the k -th nearest neighbor in all cases. Under this setting, on average, cases farther from the query’s k -th nearest neighbor will not be activated, as their case distances will be larger than $bias_c$. Conversely, cases within the k -th nearest neighbor will be activated.

4 Experimental Evaluation

Computational experiments are carried out to test two main hypotheses:

1. NN-kNN using glocal feature weighting retains accuracy comparable to that of NN-kNN_O using either global or individual feature weighting.
2. NN-kNN using sampling and feature extraction achieves comparable accuracy to neural counterparts on larger datasets, while providing instance-based explanations.

4.1 Settings and Implementation

To evaluate the impact of varying parameters, we test various k and w until best performance is found. The default case activation B is determined by the average distance to the k -th nearest neighbor across all cases, and w represents the number of global feature weights. All experimental results are summarized but only experimental results providing interesting insights are shown due to space.¹

For datasets with predefined train-test splits, we use the provided partitions. For datasets without such splits, we create a 90-10 train-test split. All models, including NN-kNN and the baseline models, are trained until testing accuracy stabilizes, defined as no improvement for 40 epochs (referred to as the training patience). This evaluation approach is applied consistently across all models for fair comparison. A more robust approach would train until validation accuracy plateaus within the training patience and then measure testing accuracy, but this is not feasible for smaller datasets as splitting the training set further into a validation set could significantly reduce the size of both subsets, potentially destabilizing training and leading to unreliable results.

¹All code can be found on <https://github.com/Heuzi/NN-kNN>

	features	samples	classes
Iris	4	150	3
Zebra (a)	2	110	2
Zebra (b)	2	220	2
Wine	13	178	3
Breast Cancer	30	569	2
Balance	4	625	3
Digits	64	1797	10

Table 1: Dataset Characteristics

For smaller datasets, we use 10-fold cross-validation; for larger datasets, we conduct 10 iterations on the given train-test split. The mean and standard deviation of accuracy are reported. For NN-kNN, if all training cases cannot fit into memory, we sample a subset of cases evenly across all classes.

4.2 Parameter Settings

We trained baseline models (e.g., convolutional image classifiers), with a learning rate of $1e^{-4}$. For NN-kNN without a feature extractor on small datasets (Section 5.1), we set the learning rate to $1e^{-2}$, as it provided the fastest convergence and helped avoid local minima. For NN-kNN on larger datasets, we used varying learning rates tailored to different components of the model: $1e^{-4}$ for the feature extractor, $1e^{-3}$ for the glocal weighting parameters, and $1e^{-4}$ for case-related parameters such as case $bias_c$ and $case_weight$. These choices were guided by experimental observations: the glocal weighting parameters benefit from larger steps to converge faster and avoid local minima; the feature extractor requires fine-tuning, similar to traditional neural network classifiers; and the case-related parameters need smaller learning rates to prevent early overfitting, which could overshadow the training of the rest of the model.

5 Experimental Results

5.1 Comparison with NN-kNN_O

The first experiments for classification tasks parallel those in the NN-kNN_O study [Ye *et al.*, 2024]. All data sets (see Table 1) are from UCI repository [Dua and Graff, 2017] except Zebra (a) and Zebra (b), which are explained later. Table 2 shows the classification accuracies of the models. F1 scores are not shown as the data sets are balanced and F1 shows a consistent pattern with accuracy scores. NN-kNN_O allows a few parameter settings such as whether to allow only the top k cases to contribute to class activation and whether all cases share a single global weighting or each case have its own individual weighting. For comparison, we include the previously reported best results by NN-kNN_O and a standard neural network classifier with 4 hidden layers using leakyReLU activation functions.

The most notable experimental results concern the Zebra Stripe datasets. They are two synthetic datasets, named Zebra (a) and Zebra (b), where each sample has two attributes x and y and one of two class labels, illustrated in Figure 2. In Zebra (a), only the feature x is relevant; In Zebra (b), x is relevant if $x < 100$ otherwise y is relevant. The classes are distributed

	$w=1$	$w=4$	k	NN-kNN _O	NNet
Iris	0.980 (0.031)	0.973 (0.044)	5	0.966	0.987
Zebra	0.945 (0.164)	0.964 (0.073)	1	0.918	0.782
(a)	0.800 (0.172)	0.982 (0.036)	5		
Zebra	0.764 (0.057)	0.923 (0.041)	1	0.968	0.673
(b)	0.718 (0.076)	0.932 (0.047)	5		
Wine	0.922 (0.075)	0.972 (0.038)	1	0.994	0.836
	0.838 (0.103)	0.843 (0.110)	5		
Breast Cancer	0.986 (0.019)	0.984 (0.018)	5	0.959	0.951
Balance	0.942 (0.025)	0.952 (0.032)	5	0.944	0.994
Digits	0.983 (0.008)	0.986 (0.010)	5	0.988	0.983

Table 2: Comparison between NN-kNN, NN-kNN_O, and a standard neural network (“NNet”). The mean standard deviations of accuracies are shown in parentheses. k is used to set B as average distance to k -th nearest neighbors. NN-kNN_O uses either global weighting or case individual weighting, whichever achieves higher accuracy.

interchangeably along the axis of the relevant feature. These datasets may appear deceptively simple. Standard neural networks, k-NN, NCA, LMNN all fail to capture the essence of the model and have poor accuracies (most $< 70\%$), with the exception that NCA achieved 98.1% for Zebra (a). In tests, NN-kNN manages to learn the ideal feature weights. For example, when using $w \geq 2$ on Zebra (b), it learns a feature weight that ignores x and another that ignores y .

The results suggest the following key findings:

- NN-kNN generally outperforms NN-kNN_O, except for Zebra (b) and Wine. This discrepancy arises because NN-kNN_O allows individual case weighting, which can be advantageous in scenarios where multiple local landscapes deviate significantly from the global trend.
- Increasing w consistently improves the performance of NN-kNN. Additional global weightings allow the model to adapt to more hidden patterns within the feature space.
- The choice of k has a significant impact on performance. A poorly chosen initial default bias can result in either too many or too few cases being activated, which hinders the model’s ability to learn effectively during training.

5.2 Image Classification

To test the effectiveness of NN-kNN with a feature extractor on image tasks, we carried out experiments on CIFAR-10 [Krizhevsky, 2009] and SVHN [Netzer *et al.*, 2011]. CIFAR-10 contains natural images of 10 classes such as airplanes, frogs, cats, etc., while SVHN contains images of house number digits from natural street views, also with 10 classes (one for each digit). CIFAR-10 consists of 60,000 images of dimension $3 \times 32 \times 32$ (channel \times width \times height). The dataset has a preset partition of 50,000 training samples and 10,000 testing samples. Similarly, SVHN contains images of the same dimensions as CIFAR-10 and is divided into 73,257 images

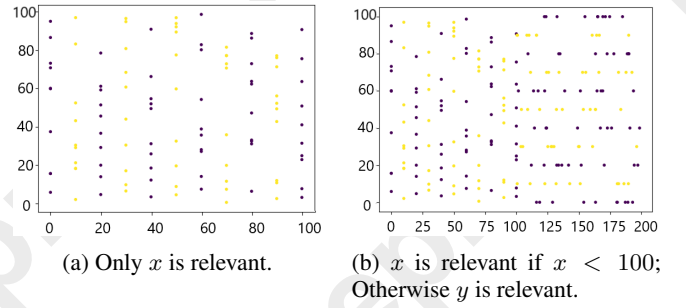


Figure 2: Deceptively simple Zebra datasets [Ye *et al.*, 2024].

Method	CIFAR-10	SVHN
Conv + NN-kNN 500	0.688 (0.006)	0.867 (0.003)
Conv + NN-kNN 2000	0.675 (0.003)	0.841 (0.008)
ConvNet	0.689	0.875
kNN	0.339	0.469
Pre-Conv + kNN	0.647	0.869
Pre-Conv + NN-kNN	0.585	0.75

Table 3: Accuracies of Different Methods on Image Classification Tasks. “Conv” stands for convolutional layer for feature extractor. “ConvNet” stands for standard convolutional neural network classifier. “Pre-Conv” stands for convolutional layer pretrained from “ConvNet” and parameters are frozen after training.

for training and 26,032 images for testing. The mean and standard deviation of all image pixels are computed across all images and channels in the training dataset. These statistics are used to standardize the pixel values for both the training and testing datasets.

For comparison, we used a convolutional neural network (CNN) with the following architecture: two convolutional layers, each followed by ReLU activation and max pooling. The first convolutional layer uses 32 filters with a kernel size of 3 and padding of 1, while the second uses 64 filters with the same configuration. After the convolutional and pooling layers, the feature map is flattened and passed through a fully connected layer with 128 units and ReLU activation, followed by a final output layer with 10 units (one for each class).

We use the layers of the CNN up to the penultimate layer as the feature extractor for both NN-kNN and vanilla k-NN. For NN-kNN, we experimented with the setting $w = 1$, $k = 20$ and sampling 500 and 2000 cases for each query. We experimented with two approaches for feature extractors of NN-kNN: using a frozen pretrained CNN, or training the CNN alongside NN-kNN from scratch. In contrast, because k-NN cannot jointly train with the feature extractor, we use a frozen pretrained CNN as the feature extractor for k-NN.

Classification Accuracy

The results are presented in Table 3. We observe that NN-kNN and ConvNet have comparable accuracy. While using a pretrained feature extractor significantly improves the performance of k-NN, NN-kNN tends to overfit when using pretrained feature extractors. This suggests that training the feature extractor jointly with NN-kNN allows it to be better op-

timized for instance-based reasoning, enabling NN-kNN to fine-tune feature weights and further enhance accuracy. Notably, “Conv + NN-kNN” performs better than “Pre-Conv + kNN” in CIFAR-10 but equally well in SVHN. We believe that this is because SVHN is an easier data set and the features extracted by pretrained “ConvNet” are sufficient for k-NN to use for instance-based reasoning.

NN-kNN also demonstrates robustness in the presence of misclassification. For instance, in one experiment on CIFAR-10, NN-kNN achieves an accuracy of 67.2%. The true class label is among the top 2 activated cases 82.02% of the time and within the top 3 classes 89.96% of the time. This highlights NN-kNN’s ability to provide meaningful predictions even when the final classification is incorrect.

Interpretability

NN-kNN provides interpretable predictions by explaining its decisions based on the activated cases. Unlike post-hoc explanations of neural network decisions by cases [Keane and Kenny, 2019], where similar cases are retrieved after a prediction is made, the activated cases in NN-kNN directly lead to the prediction. Examples of these explanations in CIFAR-10 are illustrated in Figure 3. We highlight the use of these explanations in two challenging scenarios.

1. Correct Prediction with Misleading Activated Cases:

The model makes the correct prediction due to contributions from activated cases of the correct class, but the most activated cases belong to a different class. In such instances, the activation values of the misleading cases are often lower, reflecting reduced confidence.

2. Misclassification with Plausible Activated Cases:

When the model misclassifies a query, the most activated case often belongs to the incorrect class but shares significant similarities with the query. This provides a rationale for the model’s error and misclassification.

These scenarios illustrate that NN-kNN explanations provide valuable insights into its decision-making process. We plan to conduct a formal evaluation of its interpretability in future research.

5.3 Movie Review Sentiment Analysis

To evaluate the effectiveness of NN-kNN with a feature extractor on a language task, we conducted experiments using the Stanford Sentiment Treebank (SST) dataset. The SST dataset consists of sentences extracted from movie reviews, annotated for sentiment at the phrase and sentence levels. It includes five sentiment labels: very negative, negative, neutral, positive, and very positive, commonly referred to as SST-5. The dataset contains 8,544 samples in the training set and 2,210 in the test set. Additionally, we experimented with a simpler version of the dataset, SST-2, which removes neutral comments and combines the positive and very positive labels into a single positive class, and the negative and very negative labels into a single negative class. This reduces the problem to a binary classification task. SST-2 contains 6290 training samples and 1821 testing samples.

For comparison, we took an approach similar to that in Section 5.2 by using a Bidirectional Long Short-Term Memory

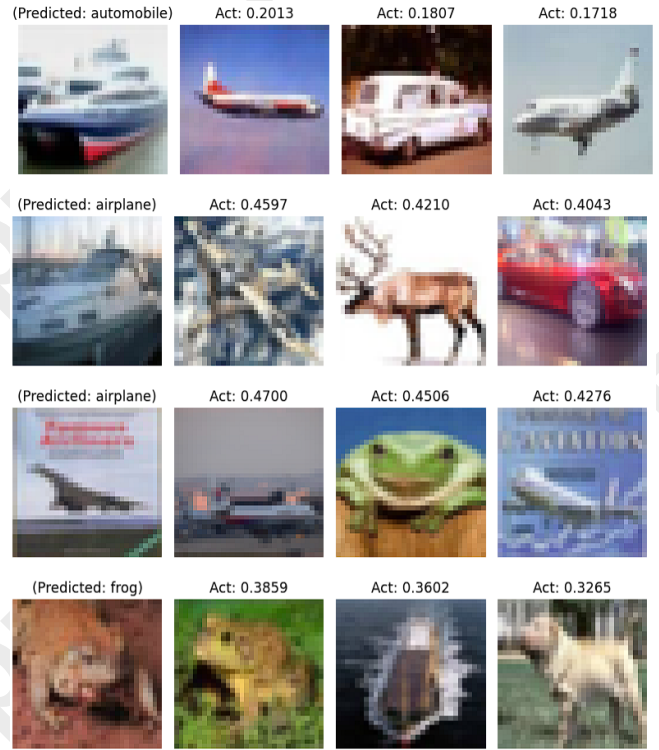


Figure 3: Instance-based explanations by NN-kNN for CIFAR-10. Each row displays a query image followed by three most activated cases. Misclassifications (row #1 and #2) are often accompanied by competing class activations, highlighting the model’s confusion between similar classes.

(Bi-LSTM) as the baseline model. The model begins with an embedding layer that projects each input token into an embedding. These embeddings are then processed by the Bi-LSTM, producing a 256-dimensional feature vector. Beyond feature extraction, the architecture incorporates a dropout layer with a rate of 0.5, followed by two fully connected layers for classification, where the intermediate layer has 64 hidden units.

In the following experiments, we use the layers of the Bi-LSTM baseline model up to the dropout component, namely, the embedding and Bi-LSTM layers, as a feature extractor for both NN-kNN and vanilla k-NN. This ensures that both models process inputs of consistent dimensionality. Specifically, we employ a pretrained Bi-LSTM feature extractor for vanilla k-NN. We test two NN-kNN configurations: one using a frozen Bi-LSTM extractor, and another where both the extractor and NN-kNN are trained jointly from scratch. In all NN-kNN experiments, we set $w = 4$, $k = 5$, and sample 500 cases for each query.

Table 4 shows our results. In SST-5, although “Bi-LSTM” is the best performing model, pretrained Bi-LSTM works well with kNN. NN-kNN outperforms kNN using either a Bi-LSTM pretrained or trained from scratch. In SST-2, “PreBi-LSTM + kNN” unexpectedly surpasses the baseline “Bi-LSTM”. Furthermore, “PreBi-LSTM + NN-kNN” achieves the highest performance, surprisingly outperforming “Bi-

Method	SST-5	SST-2
Bi-LSTM	0.376	0.776
PreBi-LSTM + kNN	0.352	0.782
PreBi-LSTM + NN-kNN	0.363 (0.002)	0.785 (0.001)
Bi-LSTM + NN-kNN	0.368 (0.007)	0.763 (0.003)

Table 4: Accuracies of different methods on SST-5 and SST-2 datasets. “Bi-LSTM” is the baseline Bi-LSTM classifier. “PreBi-LSTM” stands for Bi-LSTM pretrained from “Bi-LSTM” and parameters are frozen after training. “Bi-LSTM + NN-kNN” has a Bi-LSTM feature extractor trained along NN-kNN.

Query 1: A taut , intelligent psychological drama .	2 (predicted: 2)
A poignant and gently humorous parable that loves its characters and communicates something rather beautiful about human nature .	2 0.2551
A dark , quirky road movie that constantly defies expectation	2 0.2331
Query 2: <unk>when I get this much <unk>, I like <unk>to go with it .	-1 (predicted: 0)
<unk>John McKay is never able to pull it back on course .	-1 0.1710
A very capable <unk>.	1 0.1544
Query 3: I loved looking at this movie	1 (predicted: 1)
I loved this film .	2 0.4730
I think it was <unk>who said , ' I think , therefore I know better than to rush to the theatre for this one . '	-1 0.1676

Table 5: Instance-based Explanation by NN-kNN for SST-5. <unk> stands for unknown token ignored by feature extraction. Each query is followed by the top two activated cases. Labels are integers in $[-2, 2]$. The query’s true label and predicted class are shown in the right column. Each activated case’s true label and its activation are shown beside the case.

LSTM + NN-kNN.” However, the differences in performance across models in SST-5 and SST-2 are relatively small. We hypothesize that Bi-LSTM extracts meaningful features that work particularly well with k-NN, leaving limited room for NN-kNN to provide improvement when trained jointly.

Some sample explanations provided by NN-kNN on SST-5 are shown in Table 5. Some explanations are intuitive and obvious, for example, query #3 “I loved looking at this movie” is very similar to its top activated case “I loved this film” with a high activation. Some explanations are less so, for example, query #2 is activating cases of multiple classes, all with lower activations. This reflects the model’s confusion on query #2, which is indeed difficult to classify even for humans.

5.4 Discussion of Experimental Results

In summary, NN-kNN demonstrates accuracy comparable to its neural network counterparts across various datasets, while providing meaningful, instance-based explanations for its predictions. By using subsets of samples in training and inference, NN-kNN effectively combines general pattern knowledge (weights and bias) and instances (cases), and scales to larger datasets without sacrificing accuracy.

Even when NN-kNN misclassifies, the model’s confusion is evident through competing case activations from diverse classes. For high-dimensional datasets, NN-kNN can effectively leverage feature extractors, whether pre-trained or

jointly trained from scratch with NN-kNN. However, NN-kNN carries a risk of overfitting when paired with a pre-trained feature extractor, often underperforming compared to a vanilla k-NN using the same extractor. This occurs because pre-trained extractors are not optimized for instance-based reasoning, and in our experiments, NN-kNN operates on a sampled subset of 500 cases per query rather than using all cases as in vanilla k-NN. Notably, this risk is mitigated when the feature extractor is trained jointly with NN-kNN from scratch, ensuring better alignment with instance-based reasoning objectives. That harmonization of neural and symbolic reasoning is in spirit similar to Leake and Ye [2021].

Choice of k

We experimented with various values of k and report only the best-performing settings identified through empirical trials. Ideally, k should yield a majority of same-class activations, with a few from other classes to facilitate learning from borderline cases. If k is too small, only samples from the same class are activated, resulting in minimal classification errors for the model to learn from. Conversely, if k is too large, too many cases are activated, leading to conflicting gradient directions as errors arise from samples across diverse classes. A guideline is to choose k so that generally cases share the same labels with most—but not all—of their top k neighbors.

Number of Global Feature Weights w

We experimented with higher values of w on both image and language datasets but found no significant difference compared to $w = 1$. This contrasts with the results shown in Table 2, where increasing w often led to performance improvements. The key distinction lies in the dimensionality of the features extracted in these experiments. For larger datasets, such as CIFAR-10, the feature extractors produce high-dimensional feature representations (e.g., 128 dimensions), reducing the necessity of higher w . In scenarios involving low-dimensional features, w plays a critical role by distributing information across multiple feature weightings, compensating for the limited feature space where individual features might encode multiple hidden patterns. However, for models operating on high-dimensional feature spaces, the luxury of abundant feature dimensions diminishes the utility of w , as the extracted features are already sufficiently expressive to capture complex patterns.

6 Conclusion

With its flexibility, scalability, and interpretability, NN-kNN is a promising architecture for interpretable machine learning. Our experiments illustrate that NN-kNN can be combined effectively with feature extractors using neural methods such as convolutional layers and LSTMs, providing good accuracy. Because an important benefit of kNN is its simple incremental learning, a future research direction is to develop an incremental learning version of NN-kNN. We hypothesize that similar cases follow consistent local weighting patterns, and, consequently, that a new case can be assigned its neighboring cases’ global feature weighting. This would enable NN-kNN to incorporate a new case by adding it directly to the case layer, without retraining network parameters.

Acknowledgements

We thank the DeepCBR group at Indiana University Bloomington for their collegial support and exchange of ideas.

Contribution Statement

Authors are listed by level of contribution. Ye made major contributions to all aspects including writing, implementation and experiments. Leake contributed ideas, designs, and direction, and substantial writing. Wang was heavily involved in most implementation and all experiments. Crandall provided regular consultations on ideas and direction.

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