

Identifying and Reusing Learnwares Across Different Label Spaces

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Abstract

The *learnware paradigm* focuses on leveraging numerous established high-performing models to solve machine learning tasks instead of starting from scratch. As the key concept of this paradigm, a learnware consists of a well-trained model of any structure and a specification that characterizes the model’s capabilities, allowing it to be identified and reused for future tasks. Given the existence of numerous real-world models trained on diverse label spaces, effectively identifying and combining these models to address tasks involving previously unseen label spaces represents a critical challenge in this paradigm. In this paper, we make the first attempt to identify and reuse effective learnware combinations for tackling learning tasks across different label spaces, extending their applicability beyond the original purposes of individual learnwares. To this end, we introduce a statistical class-wise specification for establishing similarity relations between various label spaces. Leveraging these relations, we model the utility of a learnware combination as a minimum-cost maximum-flow problem, and further develop fine-grained learnware identification and assembly methods. Extensive experiments with thousands of heterogeneous models validate our approach, demonstrating that reusing identified learnware combinations can outperform both training from scratch and fine-tuning a generic pre-trained model.

1 Introduction

Machine learning has achieved significant success in various practical fields, including medicine, robotics, and ecology. However, in classic machine learning paradigm, training a well-performing model from scratch still requires several challenging conditions, such as sufficient labeled data, adequate computational resources, and proficient training skills. Additionally, privacy and proprietary concerns obstruct data sharing among developers, limiting the potential of big models in many data-sensitive scenarios.

To tackle these issues simultaneously, *learnware* [Zhou, 2016; Zhou and Tan, 2024] was proposed for solving ma-

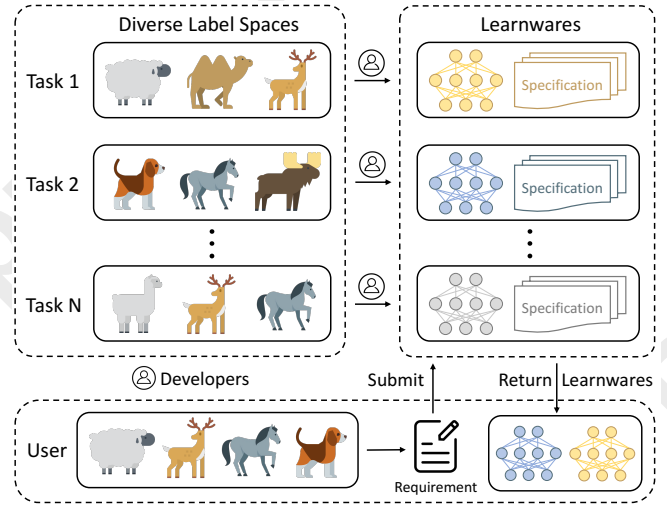


Figure 1: Given the existence of numerous learnwares from diverse label spaces, a critical challenge is to effectively identify and reuse helpful learnware combinations to address user tasks involving previously unseen label spaces.

chine learning tasks in a novel paradigm. In this context, a learnware consists of a well-performing model of any structure and a *specification* which captures the model’s specialty and utility in a certain representation, such as its statistical properties. Developers worldwide can submit their models trained on various tasks into a *learnware dock system* spontaneously, and the system helps generate specifications for each model to form learnwares. When facing a new user task, the system can identify and assemble helpful learnwares from all existing learnwares based on their specifications. The user can then reuse these learnwares with her own data to address her task instead of starting from scratch. It is important to note that the learnware dock system should not access the raw data of either model developers or users.

To realize the vision depicted above, the critical challenge of learnware paradigm is to effectively identify and assemble useful learnwares within a learnware dock system for new user tasks, without accessing raw data. The key to the solution is *specification*, the core of this paradigm. Recently, the reduced kernel mean embedding (RKME) specification [Zhou and Tan, 2024] was proposed, characteriz-

ing model capabilities via distribution information. Based on this specification, several learnware search and reuse algorithms have been developed, and the efficacy of specification-based model selection and combination has been empirically and theoretically verified [Wu *et al.*, 2023; Liu *et al.*, 2024; Tan *et al.*, 2024a]. However, considering that numerous existing models and future user tasks come from diverse label spaces, an important problem in the learnware paradigm is still unsolved: *how to identify and reuse helpful learnware combinations for user tasks across different label spaces*, which greatly limits the scope of the learnware dock system. To illustrate, consider a scenario shown in Figure 1, where a user needs to classify classes such as sheep, deer, horses, and dogs. Although the system does not possess a single learnware trained specifically for classifying these four classes, there exists a learnware combination whose label spaces collectively encompass the user’s required label space. If these relevant learnwares can be identified and combined to address the user task, it would significantly expand the scope of user tasks that can be handled, enabling the reuse of the combination beyond the limits of individual learnwares. With the initial learnware dock system recently built [Tan *et al.*, 2024b], tackling this problem has become more crucial.

In practice, the fundamental challenges of this problem mainly stem from two aspects: the unknown correspondence between different label spaces of learnwares and the user task, and the inability of the system to access raw data from model developers or users. Although accurate semantic information about each label space would make the problem easier, obtaining such information is particularly difficult due to the inherent ambiguity of natural language, the enormous number of learnwares in the system, and the additional complexity imposed on users in describing their requirements.

In this paper, to overcome these challenges without leveraging semantic information, our key insight is to represent model capabilities with statistical class-wise specifications and model the utility of a learnware combination to a user task from a perspective of class matching, thereby establishing relations between label spaces of each learnware and user tasks. Based on these relations, the system can handle user tasks involving previously unseen label spaces by identifying and assembling effective learnware combinations without access to raw user data. These learnwares collectively cover the required label space, providing an effective solution. The main contributions are summarized as follows:

- We make the first attempt to identify helpful learnware combinations across different label spaces to solve user tasks involving previously unseen label spaces, without accessing raw data from model developers or users. This enables the reuse of these combinations beyond the original purposes of individual learnwares, significantly expanding the scope of user tasks that can be handled.
- To represent a model’s capabilities on each class, we extend the RKME specification into a class-wise version, capturing the conditional distribution and measuring similarity relations between different label spaces. Leveraging these relations, we model learnware combination utility for user tasks as minimum-cost maximum-

flow problems, and further develop practical methods for identifying and reusing useful learnware combinations.

- Extensive experiments involving thousands of heterogeneous models validate the efficacy of our approach. Empirical results also show that reusing identified learnware combinations can outperform both training from scratch and fine-tuning a generic pre-trained model.

2 Problem Setup

The learnware paradigm consists of two stages: the submitting and deploying stages.

Submitting Stage. In this stage, N developers submit their models $\{f_i\}_{i=1}^N$ to the learnware dock system. Each model f_i is trained on a dataset $D_i = (\mathbf{X}_i, \mathbf{y}_i)$ over $\mathcal{X} \times \mathcal{Y}_i$, where \mathcal{Y}_i denotes the label space unique to model f_i . In settings with heterogeneous label spaces, each model’s label space \mathcal{Y}_i can be distinct. Additionally, along with the well-trained model f_i , each developer also provides a specification S_i to the system, which is generated with assistance from the system.

Deploying Stage. In this stage, the user possesses an unlabeled dataset $D_u = \mathbf{X}_u$ defined over \mathcal{X} , and the label space associated with her task is \mathcal{Y}_u , which differs from that of all learnwares, i.e., $\mathcal{Y}_u \notin \{\mathcal{Y}_i\}_{i=1}^N$. Since there are various label spaces in the system, the user also has limited m labeled instances for each class in \mathcal{Y}_u . To tackle D_u , the user submits task requirements R_u to the system, which then returns a helpful learnware combination $\{f_i \mid i \in I\}$ with the number constraint $|I| \leq M$ based on specifications $\{S_i\}_{i=1}^N$. Subsequently, the user can solve her task by reusing these learnwares. The constraint about $|I|$ is natural and practical since the computing resources and time required for reusing learnwares are directly proportional to the number of learnwares.

Note that the learnware dock system cannot access raw data of either model developers or users. Besides, due to the decoupling of heterogeneous features and labels, identifying heterogeneous models typically requires finding a unified feature space [Tan *et al.*, 2023; Tan *et al.*, 2024a] before addressing diverse label spaces. Thus, this study assumes all models operate in a unified feature space \mathcal{X} and can naturally expand to heterogeneous feature and label spaces in the future.

3 Our Approach

In this section, we first introduce the statistical class-wise specification, which characterizes model capabilities on different classes. Building on this, we then detail our comprehensive solution, focusing on algorithms for learnware identification and reuse.

3.1 Characterizing Model Capabilities

To effectively identify and assemble suitable model combinations across heterogeneous label spaces, the first step is to precisely characterize model capabilities on different classes. However, the lack of access to raw data from model developers or users poses a significant challenge.

The cornerstone of our solution is *specification*. While the RKME specification [Zhou and Tan, 2024] has shown efficacy in several learnware studies [Liu *et al.*, 2024; Tan *et al.*,

2024a] by capturing the entire data distribution, the recent implementation [Wu *et al.*, 2023] falls short in modeling the conditional data distribution for each class, restricting its efficacy in heterogeneous label space settings. To address this, we extend RKME into a class-wise version, the *class-wise RKME specification*, incorporating conditional distribution information and enabling accurate characterization of model capabilities on each class without exposing raw data.

Let $\Delta^n = \{\beta \in \mathbb{R}^n \mid \mathbf{1}^\top \beta = 1, \beta \geq 0\}$ denote the n -dimensional simplex. For each class $c \in \mathcal{Y}$, let $\mathbf{X}_c = [\mathbf{x}_{c,1}; \mathbf{x}_{c,2}; \dots; \mathbf{x}_{c,m_c}]$ represent the subset of dataset D belonging to class c and correctly classified by model f . Then the *class-wise RKME specification* $S = \{(\beta_c \in \Delta^n, \mathbf{Z}_c \in \mathcal{X}^n)\}_{c \in \mathcal{Y}}$ is generated by solving:

$$\min_{\{\beta_c, \mathbf{Z}_c\}_{c \in \mathcal{Y}}} \sum_{c \in \mathcal{Y}} \left\| \hat{\mu}_c - \sum_{j=1}^n \beta_{c,j} k(\mathbf{z}_{c,j}, \cdot) \right\|_{\mathcal{H}_k}^2, \quad (1)$$

where $k : \mathcal{X} \times \mathcal{X} \mapsto \mathbb{R}$ is a kernel function with reproducing kernel Hilbert space \mathcal{H}_k , and $\hat{\mu}_c = \frac{1}{m_c} \sum_{i=1}^{m_c} k(\mathbf{x}_{c,i}, \cdot)$ is the empirical KME [Smola *et al.*, 2007] of class c . The reduced set size n , much smaller than the size of original dataset D , is empirically set to 10 in experiments. Inspired by [Wu *et al.*, 2023], we solve Eq. (1) using alternating optimization: β_c is updated via quadratic programming, while \mathbf{Z}_c is optimized using gradient descent, as detailed in Algorithm 1.

Since the specification S is an extension of RKME across different classes, it retains the properties of RKME, such as protecting original data and providing robust defense against common inference attacks [Lei *et al.*, 2024]. Furthermore, it incorporates conditional distribution information, as demonstrated in the following proposition with proof in Appendix C.

Proposition 1. Assume $\sup_{\mathbf{x} \in \mathcal{X}} k(\mathbf{x}, \mathbf{x}) < \infty$. Let $\tilde{\mu}_c = \sum_{j=1}^n \beta_{c,j} k(\mathbf{z}_{c,j}, \cdot)$. Then, $\forall c \in \mathcal{Y}$, we have $\|\hat{\mu}_c - \tilde{\mu}_c\|_{\mathcal{H}_k} = \mathcal{O}(n^{-1/2})$, where n is the reduced set size of specification S .

As the empirical KME $\hat{\mu}_c$ captures the conditional distribution information of data correctly classified as class c by model f [Smola *et al.*, 2007], Proposition 1 indicates that the specification S accurately characterizes model capabilities on different classes, enabling precise learnware identification. In the submitting stage, each developer generates the *class-wise RKME specification* S_i with system assistance and submits the learnware (f_i, S_i) without disclosing their raw data.

3.2 Identifying Helpful Learnware Combinations

In the deploying stage, the user submits task requirements R_u to the system, expecting to receive helpful learnwares $\{f_i\}_{i \in I}$ for her task D_u , without leaking raw data. To achieve this, we first delve into the design of user task requirements and then present a practical learnware identification method.

User Task Requirements. Similar to model developers, the user can locally generate the *class-wise RKME specification* S_u using her limited m labeled data per class in \mathcal{Y}_u . To better capture the task’s statistical properties, we further enhance the requirements R_u by estimating class probabilities.

For the user task, let $\mathbf{X}_u \in \mathcal{X}^{m_u}$ be the unlabeled dataset and $\{\mathbf{X}_c \in \mathcal{X}^{m_c}\}_{c \in \mathcal{Y}_u}$ the labeled dataset. Utilizing kernel mean embedding techniques [Smola *et al.*, 2007], we can estimate class probabilities $\mathbf{w} \in \Delta^{|\mathcal{Y}_u|}$ by solving the following

Algorithm 1 Specification Generation

Input: Local dataset D with label space \mathcal{Y} , model f , kernel function k , specification size n , iteration T .

Output: The class-wise RKME specification S .

- 1: **for** $c \in \mathcal{Y}$ **do**
- 2: Obtain the data \mathbf{X}_c in D that is correctly classified by model f as class c . Initialize \mathbf{Z}_c by running k -means clustering on \mathbf{X}_c with the number of clusters set to n .
- 3: **for** $t = 1$ **to** T **do**
- 4: Update $\beta_c^{(t)}$ by using standard quadratic programming tools to minimize Eq. (1).
- 5: Update $\mathbf{Z}_c^{(t)}$ by optimizing Eq. (1) with the gradient descent method.
- 6: **end for**
- 7: **end for**
- 8: $S \leftarrow \{(\beta_c^{(T)}, \mathbf{Z}_c^{(T)})\}_{c \in \mathcal{Y}}$.

Algorithm 2 Multiple Learnware Identification

Input: Learnwares $\{(f_i, S_i)\}_{i=1}^N$, user’s local dataset \mathbf{X}_u and $\{\mathbf{X}_c\}_{c \in \mathcal{Y}_u}$, constants M, K, λ .

Output: Identified models $\{f_i\}_{i \in I}$.

- 1: Based on the local dataset, the user generates specification S_u by solving Eq. (1) and estimates class probabilities \mathbf{w} by solving Eq. (2), then submits task requirements $R_u = (S_u, \mathbf{w})$ to the system.
- 2: Initialize $I \leftarrow \{\}$, $I_0 \leftarrow \{\}$ and $\mathcal{U}(I_0, R_u) \leftarrow 0$.
- 3: **for** $t = 1$ **to** M **do**
- 4: Obtain I_t by solving Eq. (4) with the successive shortest path algorithm applied to the minimum-cost maximum-flow formulation of $\mathcal{U}(I_t, R_u)$.
- 5: If $\mathcal{U}(I_t, R_u) > \mathcal{U}(I, R_u)$ then $I \leftarrow I_t$; else exit loop.
- 6: **end for**
- 7: The system returns the helpful models $\{f_i\}_{i \in I}$.

problem via standard quadratic programming tools:

$$\min_{\mathbf{w} \in \Delta^{|\mathcal{Y}_u|}} \left\| \hat{\mu} - \sum_{c \in \mathcal{Y}_u} \frac{w_c}{m} \sum_{j=1}^m k(\mathbf{x}_{c,j}, \cdot) \right\|_{\mathcal{H}_k}^2, \quad (2)$$

where $\hat{\mu} = \frac{1}{m_u} \sum_{i=1}^{m_u} k(\mathbf{x}_{u,i}, \cdot)$ is the empirical KME of \mathbf{X}_u , and k is the kernel function from Eq. (1). The specification S_u and the class probabilities \mathbf{w} together form the user requirements $R_u = (S_u, \mathbf{w})$, which describe statistical properties of the user task without exposing raw data, laying the foundation for establishing the relations between the heterogeneous label spaces of learnwares and the user task.

Learnware Identification. After receiving the requirements, the system is required to identify a useful learnware combination for the user task. Let $\mathcal{U}(I, R_u)$ denote the utility of a set of learnwares $\{f_i\}_{i \in I}$ to the user requirements R_u , and the learnware identification process can be formulated as

$$\max_{I \subseteq [N], |I| \leq M} \mathcal{U}(I, R_u). \quad (3)$$

To quantify $\mathcal{U}(I, R_u)$, we first measure the class similarity via the class-wise specification. Let $S_i = \{(\beta_{c_1} \in \Delta^n, \mathbf{Z}_{c_1} \in \mathcal{X}^n)\}_{c_1 \in \mathcal{Y}_i}$ and $S_u = \{(\beta_{c_2} \in \Delta^n, \mathbf{Z}_{c_2} \in \mathcal{X}^n)\}_{c_2 \in \mathcal{Y}_u}$ denote the specifications for the i -th learnware and the user task.

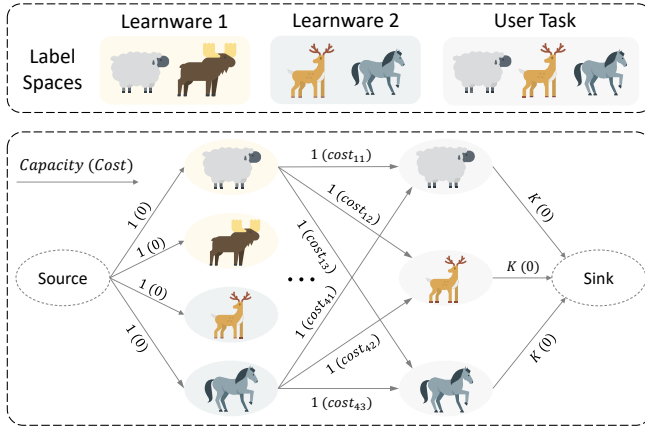


Figure 2: An illustration of modeling the utility of a learnware combination to the user task as a minimum-cost maximum-flow problem.

The similarity between class c_1 of the learnware and class c_2 of the user task, denoted as $\text{sim}(S_{i,c_1}, S_{u,c_2})$, is defined as:

$$\lambda - \left\| \sum_{j=1}^n \beta_{c_1,j} k(z_{c_1,j}, \cdot) - \sum_{j=1}^n \beta_{c_2,j} k(z_{c_2,j}, \cdot) \right\|_{\mathcal{H}_k}^2,$$

where constant λ ensures non-negative similarity, and the latter term represents the Maximum Mean Discrepancy (MMD) between two RKMEs in RKHS \mathcal{H}_k . According to Proposition 1, this term quantifies the difference between the conditional distributions of the two classes.

Based on the similarity, we quantify $\mathcal{U}(I, R_u)$ from a perspective of class matching, aiming to identify learnwares whose combined label space fully covers the task label space. Specifically, we construct a bipartite graph with learnware classes on the left and user task classes on the right. The edge weight between class c_1 of learnware f_i and user class c_2 is $w_{c_2} \cdot \text{sim}(S_{i,c_1}, S_{u,c_2})$, where w_{c_2} is the estimated probability of class c_2 . Since each user class may have multiple similar learnware classes, we constrain that each user class can be matched by at most K learnware classes. Let variable $e_{c_1,c_2}^{(i)}$ indicate whether class c_1 of learnware f_i is matched to user class c_2 . Then, the quantification of $\mathcal{U}(I, R_u)$ is modeled as the following optimization problem:

$$\begin{aligned} \max \quad & \sum_{i \in \mathcal{I}, c_1 \in \mathcal{Y}_i} \sum_{c_2 \in \mathcal{Y}_u} e_{c_1,c_2}^{(i)} \cdot w_{c_2} \cdot \text{sim}(S_{i,c_1}, S_{u,c_2}) \\ \text{s.t.} \quad & \sum_{c_2 \in \mathcal{Y}_u} e_{c_1,c_2}^{(i)} \leq 1, \quad \forall i \in \mathcal{I}, \forall c_1 \in \mathcal{Y}_i, \\ & \sum_{i \in \mathcal{I}, c_1 \in \mathcal{Y}_i} e_{c_1,c_2}^{(i)} \leq K, \quad \forall c_2 \in \mathcal{Y}_u, \\ & e_{c_1,c_2}^{(i)} \in \{0, 1\}, \quad \forall i \in \mathcal{I}, \forall c_1 \in \mathcal{Y}_i, \forall c_2 \in \mathcal{Y}_u. \end{aligned}$$

To solve this optimization problem, we transform it into an equivalent minimum-cost maximum-flow problem by treating the constraints as edge capacities and the negated edge weights as costs, as shown in Figure 2. The minimum cost can then be determined using the successive shortest path algorithm [Edmonds and Karp, 1972]. By taking the negative of this value, we obtain the maximum weight matching, which corresponds to the utility $\mathcal{U}(I, R_u)$. Further details of this modeling are provided in Appendix B.

Even with $\mathcal{U}(I, R_u)$ quantified, the problem in Eq. (3) remains NP-hard. To solve it practically, we employ a greedy algorithm to iteratively optimize Eq. (3). Specifically, at the t -th iteration, $I_t = I_{t-1} \cup \{i\}$ is obtained by solving:

$$\max_{i \in [N], i \notin I_{t-1}} \mathcal{U}(I_{t-1} \cup \{i\}, R_u). \quad (4)$$

The entire process of learnware identification is detailed in Algorithm 2, and its efficiency is analyzed in the following theorem, with the proof provided in Appendix C.

Theorem 1. Assume the maximum size of the learnware label spaces $\max_{i \in [N]} |\mathcal{Y}_i| \leq C_f$ and the size of the user task label space $|\mathcal{Y}_u| = C_u$. The time complexity of our learnware identification method is $\mathcal{O}(NC_f C_u^2 \log(C_f + C_u))$.

Since C_f and C_u are typically treated as constants, the time complexity of our method scales linearly with N , the dominant term. In contrast, the existing method [Wu *et al.*, 2023] for identifying multiple homogeneous learnwares has a time complexity of $\Omega(N^2)$, highlighting the efficiency of ours. Several methods can further accelerate our identification process. For instance, in the optimization of Eq. (4), traversing all indices $i \in [N]$ can be sped up via parallel computing. Additionally, techniques such as anchor learnwares [Zhou and Tan, 2024; Xie *et al.*, 2023] and specification index [Liu *et al.*, 2024] can substantially reduce the number of candidate learnwares N , further enhancing identification efficiency.

3.3 Reusing Learnware Combinations

While the identification phase seeks to provide learnwares whose combined label space covers the task label space, the reuse phase focuses on aligning and assembling these learnwares with the user task in a fine-grained manner. This assembly can be achieved by learning from the user’s local labeled data, naturally excluding the need for learnware specifications during reuse and further protecting developer data privacy. Since effective reuse methods vary greatly with model structure, we design practical methods tailored for both non-deep and deep learning models, ensuring broad applicability.

Let $\{f_i : \mathcal{X} \mapsto \mathbb{R}^{|\mathcal{Y}_i|}\}_{i \in \mathcal{I}}$ be the identified learnwares with diverse label spaces. For non-deep learning models (e.g., linear and tree-based), we employ methods inspired by stacking [Wolpert, 1992] and classifier adaptation [Li *et al.*, 2013]. Specifically, we augment the original features with logit vectors predicted by learnwares, which represent class probabilities. For instance, if \mathbf{X} is the raw data and $\mathcal{I} = \{1, 2\}$, the augmented data are $\mathbf{X}' = [\mathbf{X}, f_1(\mathbf{X}), f_2(\mathbf{X})]$, and a simple secondary classifier (e.g. logistic regression) is then trained on \mathbf{X}' . For deep learning models, each learnware is fine-tuned by freezing all layers except the last. Then an average ensemble method [Zhou, 2025] is applied, which averages the outputs of all learnwares for final predictions.

These proposed methods are computationally efficient with few learnable parameters. Moreover, they remain effective and robust even with limited labeled data, and improve continuously with more instances, as validated in Section 4.

4 Experiments

In this section, we develop thousands of models with diverse label spaces, spanning 22 real-world tabular and image sce-

Scenario	#Task Classes	#Models	Random	From-scratch	Linear-proxy	RKME-task	RKME-instance	Ours
CJS	6	20	99.23 ± 0.37	97.12 ± 1.20	99.32 ± 0.26	99.15 ± 0.64	99.54 ± 0.40	99.64 ± 0.00
First-Order	6	20	81.43 ± 1.94	89.27 ± 2.88	80.47 ± 5.61	85.45 ± 1.33	96.41 ± 2.23	97.96 ± 1.41
Coverttype	7	35	53.45 ± 2.52	38.71 ± 2.81	66.71 ± 13.3	80.85 ± 3.62	90.45 ± 2.16	98.79 ± 0.53
Fabert	7	35	39.78 ± 0.62	11.33 ± 0.00	41.73 ± 2.31	30.29 ± 1.22	61.03 ± 1.44	65.48 ± 1.81
Steel-Fault	7	35	75.50 ± 5.11	83.32 ± 3.27	87.16 ± 2.92	84.50 ± 3.06	95.55 ± 0.92	97.03 ± 1.30
MiceProtein	8	56	92.72 ± 2.04	84.26 ± 2.91	91.48 ± 1.93	92.50 ± 1.93	93.52 ± 0.83	95.65 ± 1.19
Otto-Product	9	84	47.53 ± 3.17	47.71 ± 2.56	51.98 ± 5.37	54.71 ± 7.68	67.97 ± 5.58	84.60 ± 2.83
Volkert	10	120	90.79 ± 2.17	80.00 ± 1.87	91.84 ± 1.35	89.95 ± 1.26	94.90 ± 0.78	96.28 ± 1.16
CTG	10	120	61.22 ± 2.45	64.05 ± 2.74	67.16 ± 4.90	61.07 ± 3.13	71.81 ± 1.53	82.51 ± 1.03
HAR	12	220	92.84 ± 1.50	91.29 ± 1.37	93.12 ± 0.79	93.45 ± 1.78	92.93 ± 2.38	97.64 ± 0.28

Table 1: Average accuracy (%) on user tasks covering all classes in tabular scenarios. Each user task includes 10 labeled instances per class. The evaluations are repeated five times, and the results are presented as the mean and standard deviation. The best is emphasized in bold.

Scenario	#Task Classes	#Users	Random	From-scratch	Linear-proxy	RKME-task	RKME-instance	Ours
CJS	[4, 5]	21	99.42 ± 0.07	90.10 ± 1.76	99.34 ± 0.19	99.47 ± 0.05	99.56 ± 0.03	99.66 ± 0.03
First-Order	[4, 5]	21	81.21 ± 2.62	56.26 ± 2.61	83.72 ± 2.60	88.94 ± 1.05	99.55 ± 0.13	98.95 ± 0.33
Coverttype	[5, 6]	28	63.00 ± 2.22	45.01 ± 1.68	78.19 ± 3.72	82.54 ± 3.28	98.39 ± 0.40	98.10 ± 0.70
Fabert	[5, 6]	28	46.01 ± 0.42	17.64 ± 0.00	55.34 ± 1.72	51.85 ± 0.40	68.21 ± 0.95	70.05 ± 1.12
Steel-Fault	[5, 6]	28	80.31 ± 1.09	85.65 ± 0.33	90.53 ± 1.24	90.51 ± 0.54	97.03 ± 0.39	97.86 ± 0.25
MiceProtein	[6, 7]	36	93.61 ± 1.42	86.02 ± 1.24	93.73 ± 1.55	93.91 ± 1.27	97.29 ± 0.88	97.40 ± 0.53
Otto-Product	[7, 8]	45	53.04 ± 0.98	48.94 ± 0.51	59.54 ± 1.20	65.24 ± 1.46	83.27 ± 0.96	88.51 ± 0.62
Volkert	[8, 9]	55	90.80 ± 0.40	83.25 ± 0.62	92.40 ± 0.44	92.10 ± 0.22	95.58 ± 0.17	96.56 ± 0.38
CTG	[8, 9]	55	64.08 ± 1.48	63.62 ± 1.15	69.80 ± 1.32	66.83 ± 1.76	77.47 ± 1.57	84.59 ± 1.56
HAR	[10, 11]	78	93.04 ± 0.51	90.69 ± 0.77	94.96 ± 0.38	94.07 ± 0.58	94.07 ± 0.37	97.67 ± 0.23

Table 2: Average accuracy (%) on user tasks covering partial classes in tabular scenarios, with the number of classes in user tasks varying within the range specified in the #Task Classes” column. Remaining experimental settings are consistent with Table 1.

narios. We compare with existing methods and conduct ablation studies to validate the efficacy of our approach.

4.1 Experimental Setup

Here we introduce some common experimental setups.

Evaluation. For a scenario with C users, methods are evaluated by the average classification accuracy $\sum_{i=1}^C \text{Acc}_i / C$, where Acc_i is the accuracy on the i -th user’s unlabeled instances, which are unseen by all learnwares in the system.

Contenders. We compare our approach with five methods: two baselines, *Random* and *From-scratch*, and three related methods, *RKME-task* [Wu et al., 2023], *RKME-instance* [Wu et al., 2023], and *Linear-proxy* [Guo et al., 2023]. *Random* randomly selects a learnware. *From-scratch* trains a new model from scratch with user labeled data and the same training algorithm as learnwares. *RKME-task* and *RKME-instance* identify single and multiple learnwares, respectively, using basic RKME specifications. *Linear-proxy* reduces the submitted model into a linear proxy model for identification. Since these contenders cannot simultaneously handle tabular and image scenarios across different label spaces, we enhance them with the reuse methods proposed in Section 3.3.

Configuration. We set the specification size n to 10 and use a Gaussian kernel $k(\mathbf{x}_1, \mathbf{x}_2) = \exp(-\gamma \|\mathbf{x}_1 - \mathbf{x}_2\|_2^2)$ with $\gamma = 0.1$. For learnware search, K is chosen from $\{2, 3, 4\}$ for different datasets, with constants $M = 5$ and $\lambda = 100$.

4.2 Evaluation on Tabular Scenarios

Scenario Construction. For tabular scenarios, we develop 745 learnwares, each with a unique label space, derived from 10 real-world datasets on the OpenML [Vanschoren et al., 2013] platform, spanning various domains such as healthcare, industrial, and biological fields. For each dataset, we select three classes from all classes, explore all possible combinations, and train models using LightGBM [Ke et al., 2017] on

the corresponding training data. For instance, for a dataset with 10 classes, we generate $\binom{10}{3} = 120$ models. This means most classes in user tasks are unseen by any single learnware.

User Task Covering All Classes. For each dataset, we test user tasks covering all classes, with each task D_u including the test set and 10 labeled data per class from the training set. Table 1 summarizes results from five repeats, showing that our method outperforms all contenders and significantly surpasses *From-scratch*, demonstrating the advantages of reusing identified learnwares with limited labeled data.

User Task Covering Partial Classes. We further test user tasks covering subsets of all classes. For a dataset with C classes, each task includes a subset of $C - 1$ or $C - 2$ classes from the test data. For example, the HAR dataset of 12 classes yields $\binom{12}{11} + \binom{12}{10} = 78$ tasks. Table 2 reports an 8/2 win/lose record, showing our method’s efficacy even when the label spaces of user tasks and learnwares partially overlap.

User Task with Increasing Labeled Data. To further explore the benefits of our method, we test cases where labeled data per class increases from 10 to 5,000, or all available data if fewer than 5,000. Figure 3 shows that our method outperforms *From-scratch* with thousands of labeled data per class and even with all labeled data in some scenarios. This suggests that reusing identified learnwares could be more effective than training from scratch, even with sufficient data.

4.3 Evaluation on Image Scenarios

Scenario Construction. For image scenarios, we develop 300 heterogeneous learnwares from 12 real-world datasets: EuroSAT [Helber et al., 2019], SVHN [Netzer et al., 2011], CIFAR10/100 [Krizhevsky and Hinton, 2009], AID [Xia et al., 2017], Pets [Parkhi et al., 2012], Resisc45 [Cheng et al., 2017], DTD [Cimpoi et al., 2014], Food [Bossard et al., 2014], Caltech101 [Li et al., 2004], Flowers [Nilsback and

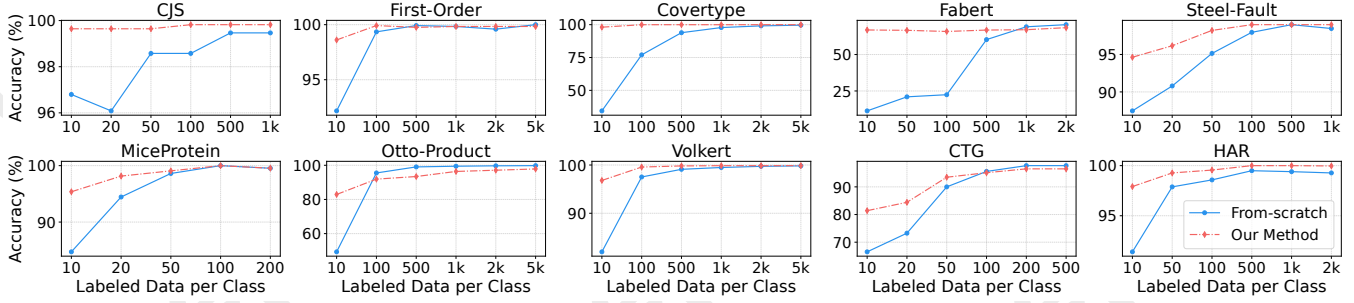


Figure 3: Average accuracy (%) on user tasks covering all classes in tabular scenarios, as the amount of labeled data per class increases.

Scenario	#Task Classes	Random	From-scratch	Linear-proxy	RKME-task	RKME-instance	ViT-ImageNet	Ours
SVHN	10	38.89 \pm 0.64	12.72 \pm 0.67	41.36 \pm 9.88	41.54 \pm 2.54	35.87 \pm 10.8	20.15 \pm 1.71	78.19 \pm 2.55
CIFAR10	10	65.54 \pm 0.53	30.18 \pm 2.91	75.92 \pm 2.15	74.87 \pm 0.73	82.61 \pm 4.70	85.44 \pm 1.16	86.20 \pm 2.64
EuroSAT	10	75.26 \pm 1.74	46.54 \pm 2.01	81.20 \pm 1.74	80.77 \pm 1.37	75.67 \pm 4.57	78.50 \pm 2.10	87.86 \pm 1.34
AID	30	76.83 \pm 0.48	60.44 \pm 1.53	81.52 \pm 0.78	80.83 \pm 0.96	85.13 \pm 1.21	71.92 \pm 1.30	87.18 \pm 0.90
Pets	37	86.41 \pm 1.02	76.84 \pm 2.28	87.23 \pm 0.56	87.10 \pm 0.81	88.34 \pm 1.32	87.32 \pm 0.37	89.28 \pm 0.75
Resisc45	45	68.62 \pm 0.44	40.32 \pm 1.77	76.32 \pm 0.64	73.45 \pm 0.75	77.06 \pm 1.01	63.79 \pm 1.14	83.42 \pm 0.95
DTD	47	55.46 \pm 0.88	47.63 \pm 1.54	59.03 \pm 0.92	56.91 \pm 1.13	61.37 \pm 0.91	55.05 \pm 0.63	62.12 \pm 1.02
CIFAR100	100	54.10 \pm 0.25	20.25 \pm 0.88	58.62 \pm 0.83	57.93 \pm 0.62	66.80 \pm 1.50	63.65 \pm 0.53	68.16 \pm 0.48
Food	101	53.21 \pm 0.50	26.26 \pm 0.64	59.00 \pm 0.38	58.38 \pm 0.29	67.32 \pm 2.09	43.64 \pm 0.85	68.49 \pm 0.80
Caltech101	101	84.91 \pm 0.65	82.38 \pm 0.60	86.45 \pm 1.66	86.52 \pm 0.94	88.62 \pm 1.03	88.47 \pm 0.85	89.38 \pm 0.99
Flowers	102	83.12 \pm 0.53	69.61 \pm 2.39	86.41 \pm 0.39	85.36 \pm 0.71	91.05 \pm 1.86	81.56 \pm 0.88	93.83 \pm 0.35
CUB2011	200	58.86 \pm 0.24	47.48 \pm 1.20	64.02 \pm 0.27	61.95 \pm 0.38	68.76 \pm 0.29	55.31 \pm 0.45	68.98 \pm 0.33

Table 3: Average accuracy (%) on user tasks covering all classes in image scenarios. Remaining details are consistent with Table 1.

Zisserman, 2008], and CUB2011 [Wah *et al.*, 2011]. These datasets span diverse domains, including plants, animals, and objects. For each dataset, we randomly select 20% to 50% of all classes and develop learnwares using corresponding training data. We perform 25 random selections per dataset, training ResNet50 [He *et al.*, 2016] models for 100 epochs using the SGD optimizer, with the initial learning rate chosen from $\{0.1, 0.01, 0.001\}$ and cosine annealing learning rate decay.

For specification generation, we use image features extracted by a generic pre-trained model, consistent with prior learnware studies [Wu *et al.*, 2023; Guo *et al.*, 2023]. Specifically, we apply a ViT-L/32 [Dosovitskiy *et al.*, 2021] model pre-trained on ImageNet [Russakovsky *et al.*, 2015]. For comparison, we introduce the *ViT-ImageNet* method, which fine-tunes the pre-trained model’s last layer with user labeled data, aligning with our reuse strategy. We also compare with other fine-tuning methods, including full parameter tuning and LoRA [Hu *et al.*, 2022], detailed in Appendix D.

User Task Covering All Classes. Consistent with Section 4.2, we test user tasks covering all classes of the test set. Table 3 shows the superiority of our method across all scenarios, suggesting that identifying and reusing small proprietary models is more effective than training from scratch or fine-tuning a generic pre-trained model in few-shot settings.

User Task Covering Partial Classes. We further test tasks covering subsets of all classes. For each dataset, we randomly select 70% to 90% of all classes, with their test data as the user task. This process is repeated ten times to generate ten unique user tasks per dataset. Table 4 shows that our method consistently outperforms others, even when the user task label space completely differs from that of existing learnwares.

User Task with Increasing Labeled Data. Consistent with Section 4.2, we test cases with increasing labeled data

per class. Figure 4 presents the superiority of our method in most scenarios, even when all labeled data are accessible.

4.4 Ablation Studies

Estimation of Class Probabilities. We compare our method using estimated probabilities w versus uniform probabilities on user tasks covering all classes. In class-balanced scenarios like CIFAR100 and Food, our method matches the accuracy of uniform probabilities. In class-imbalanced scenarios, it outperforms uniform probabilities by 6%, and in the most imbalanced scenario, Covtype, it leads by 45%. These results show the necessity of our class probability estimation.

Number of Identified Learnwares. We analyze how varying numbers of identified learnwares affect performance, as shown in Figure 5. Performance improves with more learnwares, but with diminishing returns. Reusing five learnwares generally yields satisfactory results, though cases like CTG, Otto-Product, and CIFAR100 could be further improved. In practice, the number of identified learnwares should depend on task complexity and available computational resources.

5 Related Work

Learnware. The learnware paradigm [Zhou, 2016; Zhou and Tan, 2024] proposes to build a large model platform comprising numerous high-performing models, enabling users to leverage existing models for their tasks. Each model is assigned a specification that characterizes its capabilities, allowing it to be identified for new tasks. Using the RKME specification, homogeneous learnwares can be identified by matching their data distributions with user tasks [Wu *et al.*, 2023]. This specification is proven to scarcely contain any original data and possesses robust defense against common

Scenario	#Task Classes	Random	From-scratch	Linear-proxy	RKME-task	RKME-instance	ViT-ImageNet	Ours
SVHN	[7, 9]	42.36 \pm 0.71	13.93 \pm 0.60	51.64 \pm 6.46	54.19 \pm 1.15	38.97 \pm 5.59	23.41 \pm 1.91	73.59 \pm 3.29
CIFAR10	[7, 9]	68.43 \pm 0.58	36.16 \pm 0.82	80.55 \pm 1.04	81.61 \pm 0.55	81.97 \pm 1.59	87.01 \pm 1.30	87.41 \pm 1.24
EuroSAT	[7, 9]	77.52 \pm 1.70	54.52 \pm 3.39	85.07 \pm 1.59	82.62 \pm 1.21	80.23 \pm 1.96	80.75 \pm 2.01	88.97 \pm 1.56
AID	[21, 27]	78.32 \pm 0.46	48.39 \pm 0.82	82.27 \pm 0.46	81.02 \pm 0.63	85.48 \pm 0.52	73.93 \pm 1.25	87.99 \pm 0.55
Pets	[25, 33]	88.08 \pm 0.71	79.10 \pm 1.85	88.64 \pm 0.74	88.59 \pm 0.78	90.25 \pm 0.61	88.96 \pm 0.16	90.36 \pm 0.74
Resisc45	[31, 40]	71.48 \pm 0.43	47.16 \pm 0.91	78.75 \pm 0.59	76.07 \pm 0.60	78.87 \pm 0.48	66.59 \pm 0.97	85.35 \pm 0.30
DTD	[32, 42]	58.66 \pm 0.90	51.82 \pm 0.84	61.75 \pm 0.58	60.72 \pm 0.84	63.83 \pm 1.23	58.45 \pm 0.84	65.40 \pm 1.06
CIFAR100	[70, 90]	56.97 \pm 0.24	21.16 \pm 0.74	61.69 \pm 0.58	62.14 \pm 0.36	68.87 \pm 0.70	66.46 \pm 0.48	70.85 \pm 0.50
Food	[70, 90]	55.67 \pm 0.48	29.20 \pm 0.33	61.51 \pm 0.44	61.13 \pm 0.42	69.50 \pm 0.40	45.81 \pm 0.78	70.29 \pm 0.36
Caltech101	[70, 90]	86.04 \pm 0.76	83.30 \pm 0.52	87.85 \pm 1.30	87.40 \pm 1.13	89.23 \pm 1.10	89.31 \pm 0.89	90.40 \pm 1.00
Flowers	[71, 91]	84.33 \pm 0.54	71.63 \pm 1.17	87.86 \pm 0.55	87.24 \pm 0.46	91.27 \pm 0.58	82.91 \pm 0.74	94.48 \pm 0.18
CUB2011	[140, 180]	61.84 \pm 0.21	49.23 \pm 0.61	66.88 \pm 0.31	66.31 \pm 0.17	70.88 \pm 0.39	58.22 \pm 0.52	71.43 \pm 0.23

Table 4: Average accuracy (%) on user tasks covering partial classes in image scenarios. Remaining details are consistent with Table 2.

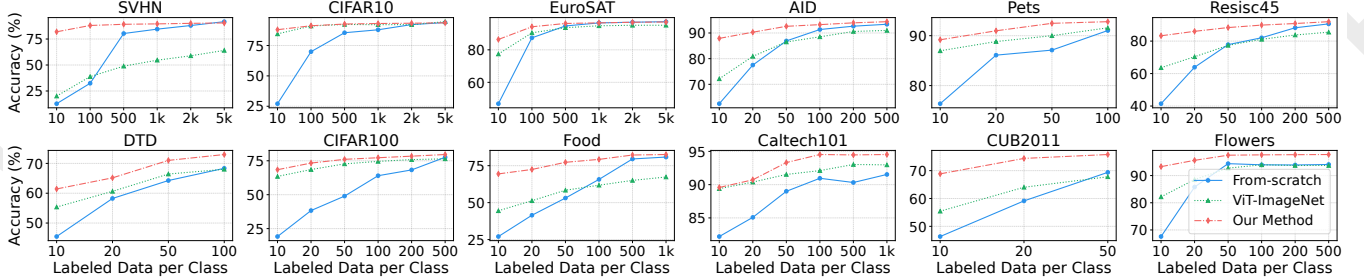


Figure 4: Average accuracy (%) on user tasks covering all classes in image scenarios, as the amount of labeled data per class increases.

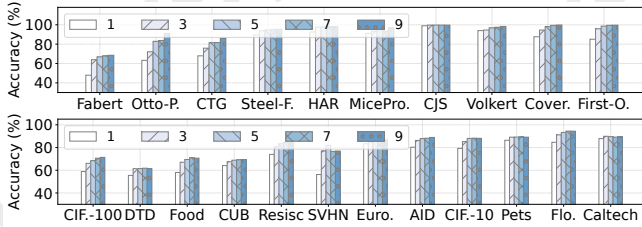


Figure 5: Average accuracy (%) on user tasks covering all classes in tabular and image scenarios, with 10 labeled instances per class, as the number of identified learnwares varies among {1, 3, 5, 7, 9}.

inference attacks [Lei *et al.*, 2024]. To support effective identification from numerous learnwares, an anchor-based mechanism [Xie *et al.*, 2023] enables efficient identification, and an evolvable learnware specification [Liu *et al.*, 2024] continuously enhances learnware characterization and identification as the system scales. For heterogeneous feature spaces, algorithms for searching and reusing learnwares are developed by learning a unified specification space [Tan *et al.*, 2023; Tan *et al.*, 2024a]. Recently, the first learnware dock system, Beimingwu [Tan *et al.*, 2024b], was released, providing implementations for the entire process of learnware paradigm.

For heterogeneous label spaces, prior work [Guo *et al.*, 2023] focuses on identifying a single learnware and requires a powerful public feature extractor, limiting its applicability especially in tabular scenarios. In contrast, our work makes the first attempt to identify and reuse effective learnware combinations across different label spaces, enabling broader applications of learnwares beyond their original purposes.

Utilizing Given Source Task(s) or Model(s). Domain adaptation [Ben-David *et al.*, 2006], transfer learning [Pan and Yang, 2010], and model reuse [Zhao *et al.*, 2020] focus on solving target tasks using given source task(s) or

model(s). Several studies also explore heterogeneous label spaces, including disjoint label space transfer learning [Luo *et al.*, 2017], open set domain adaptation [Saito *et al.*, 2018], and partial domain adaptation [Cao *et al.*, 2019]. While these fields assume the given models are helpful for the target task or require access to raw source data, the learnware paradigm differs significantly, as it aims to identify and assemble useful models from numerous ones in a data-preserving way.

Model Pools. Model pools and hubs, like Hugging Face, have rapidly grown, hosting over a million models managed with only semantic descriptions. Some works, such as HuggingGPT [Shen *et al.*, 2023] and ToolLLM [Qin *et al.*, 2024], attempt to identify models or tools via these descriptions. However, since machine learning models are functions mapping inputs to outputs, statistical specifications in the learnware paradigm are essential for capturing their implicit capabilities and enabling effective identification and reuse beyond their original purposes. Some studies also focus on assessing the reusability or transferability of pre-trained models without fine-tuning [You *et al.*, 2021; Ding *et al.*, 2022; Zhang *et al.*, 2023], but these often require running all models on user data without considering data privacy, which is impractical in real-world scenarios with numerous models.

6 Conclusion

This paper presents the first attempt to identify and assemble helpful learnware combinations for user tasks across different label spaces without leaking raw data. To achieve this, we characterize model capabilities across classes and establish relationships between diverse label spaces, proposing a practical identification and reuse method to solve user tasks involving previously unseen label spaces. Extensive empirical evaluations validate the effectiveness of our approach.

Acknowledgments

This research was supported by NSFC (62250069) and the Collaborative Innovation Center of Novel Software Technology and Industrialization. The authors would like to thank Jia-Wei Shan and Tian Qin for helpful discussions, and Zi-Chen Zhao for his participation in preliminary experiments. We are also grateful to the anonymous reviewers for their helpful comments.

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