

# Underground Diagnosis in 3D GPR Data by Learning in CuCoRes Model Space

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## Abstract

Ground Penetrating Radar (GPR) provides detailed subterranean insights. Nevertheless, underground diagnosis via GPR is hindered by the fact that training data typically contain only normal samples, along with the complexity of GPR data’s wave-collection characteristics. This paper proposes subsurface anomaly detection within the Cubic Correlation Reservoir Network (CuCoRes) model space. CuCoRes incorporates three reservoirs with spatial correlation adjustment in each direction to adequately and accurately capture multi-directional dynamics (i.e., changing information) within GPR data. Fitting GPR data with CuCoRes and representing data with fitted models, the original GPR data is mapped into a category-discriminative CuCoRes model space, where anomalies could be efficiently identified and categorized based on model dissimilarities. Our approach leverages only limited normal GPR data, easily accessible, to support subsequent anomaly detection and categorization, enhancing its applicability in practical scenarios. Experiments on real-world data demonstrate its effectiveness, outperforming state-of-the-art.

## 1 Introduction

Subsurface conditions could be effectively detected and imaged using Ground Penetrating Radar (GPR), a geophysical technique that transmits high-frequency electromagnetic (EM) waves and analyzes their reflections [Zhou *et al.*, 2018]. Compared to single-channel systems, multi-channel GPR provides richer and more detailed underground information but also produces large and complex three-dimensional (3D) GPR data<sup>1</sup> [Goodman *et al.*, 2013].

Underground diagnosis via GPR typically involves segmenting the collected GPR data along the detection direction and further identifying sections with subterranean diseases such as cracks, cavities, or looseness, a labor-intensive and time-consuming process when manually performed. While image and signal-based algorithms aid in categorizing GPR

data, they struggle with variability in anomaly characteristics such as composition, size, and environment. Advancements in Deep Learning (DL) approaches, particularly Convolutional Neural Networks (CNNs), have also been applied to object and anomaly detection in GPR data [Liang *et al.*, 2022a; Hou *et al.*, 2024]. Despite their potential, DL methods face considerations. The limited data availability, particularly in a targeted detection area, often leads to restricted training datasets primarily composed of only normal GPR data samples free from subsurface targets. The variability of underground environments also undermines the generalization of DL approaches, restricting their adaptability to various or unfamiliar subsurface conditions. These highlight the challenge of detecting and categorizing subsurface anomalies in unseen environments using only newly collected normal data.

Given the above considerations, the Learning in the Model Space (LMS) framework offers a viable alternative [Chen *et al.*, 2013]. LMS transitions data from data space to model space by fitting the data with appropriate models that capture and describe the dynamics (i.e., changing information) within the data. Consequently, the fitted models serve as more stable and parsimonious representations of the data, enabling learning algorithms to be implemented on the fitted models rather than the original data. Successfully applied to diagnosing the Barcelona water network [Quevedo *et al.*, 2014] and the Tennessee Eastman Process [Chen *et al.*, 2014], along with diverse time-series classification tasks [Gong *et al.*, 2018; Wu *et al.*, 2022], LMS has proven its efficacy in various tasks using the Echo State Network (a type of reservoir computing network) for data fitting and representation. Notably, LMS focuses on the data-intrinsic dynamics, which allows for reduced reliance on training data and diminishes the computational demands compared to many DL methodologies, particularly with adequate and accurate dynamic capture.

While efforts have been made to apply LMS in GPR data processing, considerations remain. LMS typically captures uni-directional dynamics, designed primarily for sequential data with contextual relationships. However, GPR data involves both vertical variations and horizontal correlations due to the continuity of the subsurface medium and EM waves. Although attempts have been made to adequately capture multi-directional dynamics in GPR data [Chen *et al.*, 2024; Zhou *et al.*, 2023], correlations in GPR data vary across spatial orientations due to differences in antenna channel spac-

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<sup>1</sup>“GPR data” in this paper refers to 3D GPR data by default.

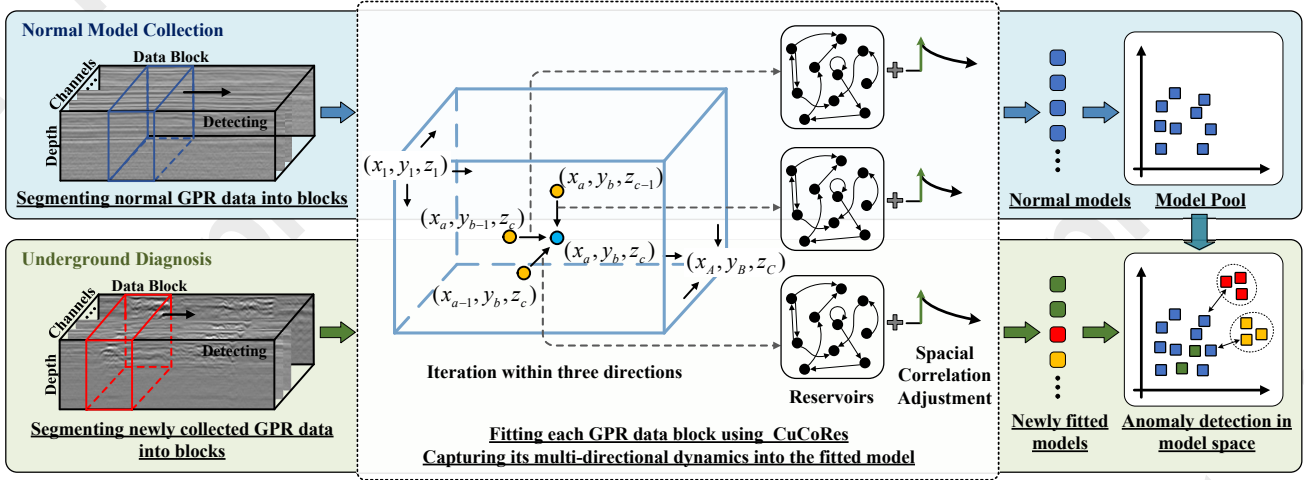


Figure 1: Our approach consists of two stages: “Normal Model Collection” and “Underground Diagnosis”. During Normal Model Collection, normal GPR data is segmented into same-sized blocks, each fitted by CuCoRes to capture its multi-directional dynamics, with the fitted models collected into the “Model Pool”. For subsequent Underground Diagnosis, the same segmentation and fitting are applied to newly collected GPR data, with fitted models compared against the model pool. Anomalies are identified and clustered based on model dissimilarities.

ing, sampling frequencies, and the underground medium’s dielectric constant, with some directions being more strongly correlated. This variation requires precise capture and adjustment of dynamics within each direction. Despite recent advances [Zhou *et al.*, 2024] to optimize this process using accurately labeled multi-type data, acquiring a sufficiently diverse training dataset often remains impractical.

In response, this paper proposes learning in the Cubic Correlation Reservoir Network (CuCoRes) model space for underground diagnosis, as depicted in Figure 1. Our approach only requires limited normal GPR data, commonly available from the detection area, to support subsequent anomaly detection and categorization. We segment normal GPR data into data blocks, with each block being fitted by CuCoRes<sup>2</sup>. Given GPR data’s vertical continuity along EM waves and horizontal correlations due to subsurface medium consistency, each point in GPR data is correlated with its surroundings in multiple directions. Different underground structures manifest different dynamics in GPR data. The proposed CuCoRes integrates three reservoirs in its hidden layer, and applies spatial correlation adjustment in each direction, constructing connections between points within the data across multiple directions, during which it adaptively strengthens the correlation with nearer points while weakening it with those further away. Fitting the data block with CuCoRes effectively captures the data-inherent multi-directional dynamics, resulting in a compact fitted readout model. Representing each block with the fitted model, coupled with the distance measurement between models, transitions the original GPR data blocks into the CuCoRes model space. These models, derived from normal data blocks, are collected into a “Model Pool”.

For subsurface anomaly detection in subsequent GPR data,

<sup>2</sup>In this paper, “CuCoRes” designates the network used for data fitting, resulting in the “CuCoRes fitted readout model” for data representation, also simplified as “CuCoRes model” or “fitted model”.

we continue with the same segmentation process and fit each data block with CuCoRes, deriving the fitted model for each block. Given the consistent dynamics within GPR data, blocks originating from identical subsurface structures derive similar CuCoRes models, whereas models fitted from diverse subsurface structures manifest significant variations, depicting the unique dynamics captured. Each newly fitted model is then evaluated against the established model pool, obtaining its anomaly score. Models registering higher anomaly scores, indicative of potential anomalies, are identified and categorized, allowing us to precisely identify the corresponding abnormal block and determine the type of anomaly associated with each identified GPR data block. The main contributions of this paper are as follows:

- Our approach focuses on the inherent dynamics present in GPR data, and leverages only limited normal GPR data, easily obtainable in the detection area, to support subsequent anomaly detection and categorization, enabling its practical usability in real-world settings.
- The introduced CuCoRes, incorporating three reservoirs with spatial correlation adjustments in each direction, builds multi-directional correlations among data points, enhancing connections with nearer points while reducing those with distant ones, thus adequately and accurately capturing multi-directional dynamics in GPR data.
- Representing data with fitted CuCoRes models, coupled with the directly computable distance measurement between models, allows further anomaly detection and categorization to be effectively performed within the category-discriminative CuCoRes model space.

## 2 Related Work

### 2.1 GPR Data Analyzing

GPR data, specifically the multi-channel 3D GPR data, provides an advanced geophysical tool for viewing what lies be-

neath the surface. As Figure 2 shows, single-channel GPR provides 2-dimensional (2D) data. Multi-channel GPR systems consist of antenna arrays, with each channel simultaneously transmitting and receiving EM waves, offering a comprehensive 3D subsurface visualization.

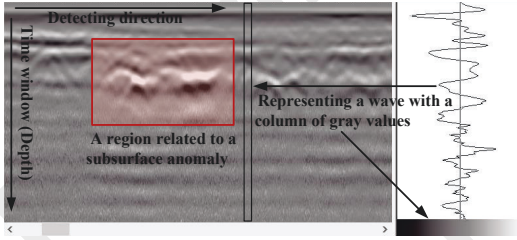


Figure 2: Single-channel GPR data is displayed in 2D format, with EM waves arranged horizontally by time or space and intensities shown in grayscale. Due to wave refraction and reflection, GPR data often requires additional analysis to accurately represent subsurface structures. In 3D GPR data, key variations occur both along and across EM waves, horizontally and vertically.

GPR data collects and arranges EM waves, with each point indicating wave intensity at a specific subsurface location. Due to the continuity of underground media and the presence of anomalies, GPR data exhibits valuable dynamics, that is, changing information vertically and horizontally along and among waves. Moreover, directional scales vary, leading to different correlations between adjacent points in various directions. For example, the distance between adjacent channels is about 15 cm, the gap between rows within a channel ranges from 2 to 6 cm, and the spacing between points within a row, influenced by the dielectric constant, is 2 to 5 cm. Accurately capturing data-inherent dynamics requires accounting for multiple directions and directional scale differences.

Recent DL advancements in 3D GPR data analysis follow two main strategies: 1) Direct 3D processing, such as Multiple Mirror Encoding (MME) [Liu *et al.*, 2022] with C3D network [Tran *et al.*, 2015] for spatio-temporal feature extraction, and 3DInvNet, which uses a 3D CNN with feature attention and a U-shaped encoder-decoder for multiscale feature aggregation; 2) Integrating 2D processing results for 3D data, such as UcNet [Kang *et al.*, 2019], combining CNNs with phase analysis to enhance resolution, and [Liang *et al.*, 2022b], comparing VGG and ResNet for classifying anomaly-associated GPR data. Nevertheless, existing DL approaches designed for 3D GPR data require multi-type labeled data for training or optimization, and fail to be performed with only limited labeled data support.

## 2.2 Learning in the Model Space(LMS)

The LMS framework<sup>3</sup>, first introduced in [Chen *et al.*, 2013], was initially applied to fault diagnosis in sequential data. LMS typically employs ESN to fit individual data instances, transitioning them into a model space represented by their respective fitted models. This transformation allows learning algorithms to operate effectively within the model space, leveraging the dynamics captured from the data. Over time,

<sup>3</sup>Also denoted as “Model-Space Learning”.

LMS has been adapted for various applications, including time series classification, disease diagnosis [Bianchi *et al.*, 2020], and addressing concept drift [Chiu and Minku, 2022].

Existing studies [Zhou *et al.*, 2023; Chen *et al.*, 2024] have investigated classifying 2D GPR data using an enhanced ESN-based network, which captures horizontal and vertical dynamics into fitted models. For 3D GPR data, characterized by higher dimensions and more complex intrinsic dynamics, a common approach is to apply LMS independently to each channel as 2D data and then aggregate the results [Liu *et al.*, 2024]. However, this approach neglects inter-channel dynamics. To address this, Zhou *et al.* [2024] proposed CubeRes, augmenting the ESN’s hidden layer with multiple reservoirs to better capture multi-directional dynamics within 3D data. Despite this, CubeRes does not a priori account for spatial scale variations across different directions in GPR data. Additionally, while this study suggested using labeled data to optimize fitting accuracy and model classification, the lack of sufficient, diverse, and accurately labeled GPR data in specific detection areas limits its practical applicability.

## 2.3 Echo State Network (ESN): A Representative Reservoir Computing Network

ESN, a subset of reservoir computing and recurrent neural networks, is renowned for its simplicity and efficiency in processing sequential data [Lukoševičius and Jaeger, 2009]. ESN features fixed, randomized input weights and a reservoir of randomly connected neurons (Figure 3). This reservoir processes historical data by transforming it into high-dimensional states, known as “echo states”, effectively capturing complex, data-inherent dynamics [Yan *et al.*, 2024].

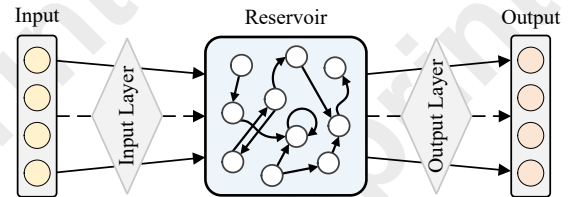


Figure 3: Typically, an ESN primarily consists of the input layer, a hidden layer containing a reservoir, and the output layer.

For sequential data fitting, ESN computes a hidden state for each point in the input sequence, and the output layer maps it to the target sequence solved via regression.

## 3 Methodology

As illustrated in Figure 1, our approach consists of two stages:

- **Normal Model Collection:** Normal GPR data, free from subsurface anomaly and readily available in the detection area, is segmented along the detecting direction into same-size blocks, each independently fitted by CuCoRes to capture its multi-directional dynamics. The resulting fitted models, representing their respective data blocks, are collected into a “Model Pool”.
- **Underground Diagnosis:** Newly collected GPR data undergoes the same segmentation and CuCoRes fitting,



obtaining fitted models. These models are compared to those in the model pool, with abnormal models identified and clustered based on model dissimilarities, enabling the detection and categorization of corresponding anomaly-associated GPR data blocks.

In our approach, fitting GPR data and capturing its multi-directional dynamics via CuCoRes are crucial for data representation and subsequent anomaly detection on fitted models. Therefore, we start with a comprehensive introduction to CuCoRes, followed by descriptions of the two stages.

### 3.1 Data Fitting and Representation via CuCoRes

CuCoRes consists of an input layer, a hidden layer, and an output layer. Notably, to accurately capture multi-directional dynamics within 3D GPR data, CuCoRes enhances the hidden layer with three reservoirs, each implementing spatial correlation adjustment, thus effectively building correlations among points in various directions.

#### Fitting GPR Data by CuCoRes

Denoting a GPR data block as  $\mathbf{U} \in \mathbb{R}^{A \times B \times C}$ , wherein a data point within this block is localized by  $(x_a, y_b, z_c)$ , and the corresponding value at that point is  $u(x_a, y_b, z_c)$ . The iteration of CuCoRes begins at the point  $(x_1, y_1, z_1)$  and ends at  $(x_A, y_B, z_C)$ . Sequentially, as shown in Figure 4, each point is sent into the hidden layer, with their hidden states  $\mathbf{h} \in \mathbb{R}^{N \times 1}$  calculated as:

$$\mathbf{h}(x_a, y_b, z_c) = g(\mathbf{W} \cdot \mathbf{E} \cdot \mathbf{h}^*(x_a, y_b, z_c) + \mathbf{W}^{\text{in}} u(x_a, y_b, z_c)), \quad (1)$$

where:

- $a, b, c \in \mathbb{Z}$  are the indices of the point  $(x_a, y_b, z_c)$  in the  $x$ -,  $y$ -, and  $z$ -directions, respectively.  $g$  is the activation function  $\tanh$ .  $\mathbf{W}^{\text{in}} \in \mathbb{R}^{N \times 1}$  denotes the input weights.
- $\mathbf{W} \in \mathbb{R}^{N \times 3N}$  are reservoir weights for each direction:

$$\mathbf{W} = [\mathbf{W}^x \quad \mathbf{W}^y \quad \mathbf{W}^z], \quad (2)$$

where  $\mathbf{W}^x, \mathbf{W}^y, \mathbf{W}^z \in \mathbb{R}^{N \times N}$  represent the reservoir weights along the  $x$ -,  $y$ -, and  $z$ -direction, respectively.

- $\mathbf{E} \in \mathbb{R}^{3N \times 3N}$  represents exponential spatial correlation adjustments applied to each direction:

$$\mathbf{E} = \begin{bmatrix} e^{-(x_a - x_{a-1})} \mathbf{I} & & \\ & e^{-(y_b - y_{b-1})} \mathbf{I} & \\ & & e^{-(z_c - z_{c-1})} \mathbf{I} \end{bmatrix}, \quad (3)$$

where  $\mathbf{I} \in \mathbb{R}^{N \times N}$  is the identity matrix,  $(x_a - x_{a-1})$ ,  $(y_b - y_{b-1})$ , and  $(z_c - z_{c-1})$  refer to the distances between a point and its adjacent points in the  $x$ -,  $y$ -, and  $z$ -direction, respectively. Introducing  $\mathbf{E}$  assigns greater importance to nearby points and reduces the influence of distant points, adaptively emphasizing local spatial relationships for more accurate dynamic capture.

- $\mathbf{h}^* \in \mathbb{R}^{3N \times 1}$  is the concatenation of the previous hidden states from the three directions:

$$\mathbf{h}^*(x_a, y_b, z_c) = \begin{bmatrix} \mathbf{h}(x_{a-1}, y_b, z_c) \\ \mathbf{h}(x_a, y_{b-1}, z_c) \\ \mathbf{h}(x_a, y_b, z_{c-1}) \end{bmatrix}.$$

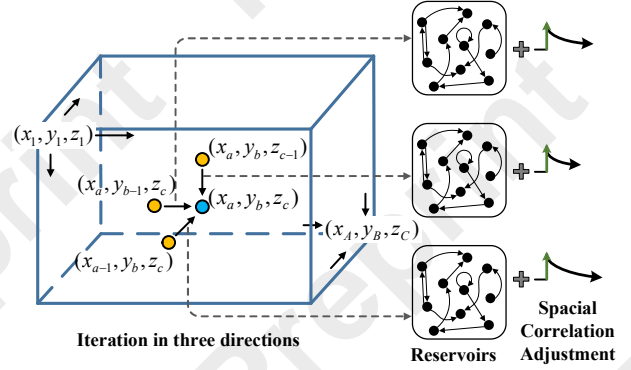


Figure 4: CuCoRes’s hidden-state iteration processes data points sequentially, starts at  $(x_1, y_1, z_1)$ , moves to  $(x_A, y_1, z_1)$ , then continues from  $(x_1, y_2, z_1)$  to  $(x_A, y_2, z_1)$ , and so forth, until reaching the end  $(x_A, y_B, z_C)$ . Each point correlates with its predecessors across three directions, with the correlation exponentially adjusted according to the distance between adjacent points in each direction.

In CuCoRes,  $\Theta = (\mathbf{W}^{\text{in}}, \mathbf{W}^x, \mathbf{W}^y, \mathbf{W}^z)$  are randomly initialized and fixed. The input weight  $\mathbf{W}^{\text{in}}$  is uniformly distributed in  $[-1, 1]$ .  $\mathbf{W}^x, \mathbf{W}^y, \mathbf{W}^z$  are randomly determined reservoir weights that describe neuron connections in the reservoir, fulfilling the Echo State Property [Jaeger, 2001], with a spectral radius within  $(0, 1)$ . The initial hidden states:  $\mathbf{h}(x_0, \cdot, \cdot) = \mathbf{h}(\cdot, y_0, \cdot) = \mathbf{h}(\cdot, \cdot, z_0) = \mathbf{0}$ .

During hidden-state iteration, each hidden state integrates current and past information, inducing directional correlations among neighboring points. The correlation adjustment  $\mathbf{E}$  modulates these correlations by strengthening connections between nearby points and weakening those between distant ones. Unlike existing LMS methods, 2D-ESN [Chen *et al.*, 2024] and C3 [Zhou *et al.*, 2023], which manually adjust directional associations, or CubeRes [Zhou *et al.*, 2024], which learns them from labeled data, our approach adapts to varying directional scales in GPR data. Evolving multi-directional correlations form a network that links each point to processed ones, accurately capturing multi-directional dynamics.

After computing the hidden states for all data points within the data block, the output value  $v$  for each point is calculated from the previous hidden states:

$$v(x_a, y_b, z_c) = \mathbf{W}^{\text{out}} \mathbf{h}^*(x_a, y_b, z_c) + \beta, \quad (4)$$

where  $\mathbf{W}^{\text{out}} \in \mathbb{R}^{1 \times 3N}$  is the output weight,  $\beta$  is the bias.

The fitting process is accomplished using the “next point prediction” task [Chen *et al.*, 2013]. It aims to predict the value of the subsequent point based on processed ones, establishing a mapping between hidden states and corresponding input data points. Explicitly, each output value  $v(x_a, y_b, z_c)$ , derived from the hidden states, is required to closely match the input  $u(x_a, y_b, z_c)$ . To achieve this, the output weights  $\mathbf{W}^{\text{out}}$  and the bias  $\beta$  are determined using ridge regression:

$$[\mathbf{W}^{\text{out}} \quad \beta]^T = (\tilde{\mathbf{H}} \tilde{\mathbf{H}}^T + \lambda^2 \mathbf{I}_{3N})^{-1} \tilde{\mathbf{H}} \mathbf{u}, \quad (5)$$

where  $\tilde{\mathbf{H}}$  is augmented from the hidden state matrix  $\mathbf{H}$ , extended by a row of ones for bias terms;  $\mathbf{H} \in \mathbb{R}^{3N \times ABC}$  is obtained by collecting the previous hidden states of all data

points in sequence and column-wise, with each column representing a specific  $\mathbf{h}^*(x, y, z)$ ;  $\mathbf{u} \in \mathbb{R}^{ABC \times 1}$  is a vectorized form of the input values  $u(x, y, z)$ , arranged in the same order as  $\mathbf{h}^*(x, y, z)$  in  $\mathbf{H}$ ;  $\mathbf{I} \in \mathbb{R}^{3N \times 3N}$  is the identity matrix; and  $\lambda$  serves as a regularization.

During CuCoRes' fitting process, the three-reservoir architecture, spatial correlation adjustments, and the unique hidden-state iteration of CuCoRes adeptly establish the correlation between adjacent points in the data block, capturing data-intrinsic changing information. The fitting approach integrates multi-directional dynamics within the data block into a compact fitted CuCoRes readout model:

$$f(\mathbf{x}) = \mathbf{W}^{\text{out}}\mathbf{x} + \beta. \quad (6)$$

This readout model provides a compact representation of the original data block. When an anomaly arises in a data block, it introduces atypical dynamics, causing the readout model to exhibit distinct characteristics compared to those derived from normal GPR data blocks. As a result, representing the data blocks by readout models enhances category discrimination, which in turn improves the effectiveness of model classification compared to using the original data blocks.

#### Distance Measurement between Fitted Models

After data fitting via CuCoRes, it is essential to establish a distance measurement to quantify the differences between the fitted models, aiding subsequent anomaly detection on the models. The  $p$ -norm distance [Chen *et al.*, 2013] between models  $f_1(\mathbf{x})$  and  $f_2(\mathbf{x})$  is adopted:

$$\mathcal{D}_p(f_1, f_2) = \left( \int_C \|f_1(\mathbf{x}) - f_2(\mathbf{x})\|^p d\mu(\mathbf{x}) \right)^{1/p}. \quad (7)$$

Here,  $f_1$  and  $f_2$  represent the simplified forms of  $f_1(\mathbf{x})$  and  $f_2(\mathbf{x})$ , respectively;  $\mu(\mathbf{x})$  denotes the probability density over the input domain, and the integral range  $C$  is  $[-1, 1]^{3N}$ . For the sake of simplicity,  $p$  is set to 2 by default, and we assume  $\mathbf{x}$  follows a uniform distribution.

Given the two blocks fitted using CuCoRes, the models derived for each are denoted as follows:

$$\begin{cases} f_1(\mathbf{x}) = \mathbf{W}_1^{\text{out}}\mathbf{x} + \beta_1, \\ f_2(\mathbf{x}) = \mathbf{W}_2^{\text{out}}\mathbf{x} + \beta_2. \end{cases} \quad (8)$$

Substituting Equation (8) into Equation (7) results in:

$$\mathcal{D}_2(f_1, f_2) \propto \frac{1}{3} \|\mathbf{W}_1^{\text{out}} - \mathbf{W}_2^{\text{out}}\|^2 + (\beta_1 - \beta_2)^2. \quad (9)$$

Such direct-measured pair-wise distance measurement specified in Equation (9) facilitates the usage of distance-based learning algorithms on the fitted models.

### 3.2 Normal Model Collection

Given normal 3D GPR data gathered from the detection area, we first segment them into same-size data blocks along the detection direction<sup>4</sup>. Each block is individually fitted by CuCoRes, resulting in a respective readout model. The models obtained from these normal blocks are collected into a

<sup>4</sup>Performed using a sliding window that moves along the detection direction, as described in [Zhou *et al.*, 2024; Liu *et al.*, 2024].

“Model Pool”. This process is described as:

$$\mathcal{M} = \bigcup_{\mathbf{r}_i \in \mathcal{R}} \{\mathcal{F}(\mathbf{U}) \mid \mathbf{U} \in \mathcal{S}(\mathbf{r}_i)\}, \quad (10)$$

where  $\mathcal{M}$  denotes the model pool,  $\mathcal{R}$  is the collection of normal GPR data samples;  $\mathbf{r}_i$  denotes a data sample in  $\mathcal{R}$ ;  $\mathcal{S}$  represents the segmentation process;  $\mathbf{U}$  is a specific data blocks; and  $\mathcal{F}$  refers to CuCoRes fitting process.

### 3.3 Underground Diagnosis

Anomaly detection on the newly collected GPR data is performed through the following three steps: **1) Fitting Data Blocks via CuCoRes:** Apply the same segmentation and fitting procedures as described earlier, obtaining the fitted CuCoRes model for each data block; **2) Model Discrimination:** For each model, find the nearest normal model in the model pool through the model distance measurement given in Equation (9), examining its anomaly score, with overly high scores identified to be anomalies; **3) Model Categorization:** Cluster the abnormal models identified in the previous step, where each cluster signifies a type of anomaly.

The first step has been previously described and is the same as the training stage, thus would not be repeated here. Details for the subsequent steps are provided as follows.

#### Distance-based Model Discrimination

For anomaly detection in newly collected GPR data, segmentation and CuCoRes fitting derive a set of fitted models (each corresponding to a data block). Each model undergoes a Nearest-Neighbor (NN) search in the model pool to estimate an anomaly score, determining its abnormality.

The existence of an underground anomaly introduces distinct dynamics that differ significantly from normal GPR data. Consequently, models fitted from such blocks deviate noticeably from those fitted from normal data, due to the distinct dynamics captured. Specifically, models derived from normal data tend to cluster tightly, while those derived from anomalies are distinctly separated from the normal ones, and positioned far from normal models. To assess the anomaly score for a newly fitted model  $f$ , the distance to its nearest neighbor model in the model pool  $\mathcal{M}$  is computed, and the anomaly score is defined as:

$$\text{score}(f) = \min_{f^* \in \mathcal{M}} \mathcal{D}_2(f^*, f). \quad (11)$$

where  $f$  is a newly fitted model,  $f^*$  denotes one of the normal models in model pool  $\mathcal{M}$ , and  $\mathcal{D}_2$  is the distance measurement between models defined in Equation (9).

A binary classifier  $\mathcal{H}$  is then employed to discriminate normal (denoted as 1) and abnormal (denoted as 0) models:

$$\mathcal{H}(f) = \begin{cases} 0 & \text{if } \text{score}(f) > \tau, \\ 1 & \text{if } \text{score}(f) \leq \tau, \end{cases} \quad (12)$$

where  $f$  represents the model under evaluation,  $\text{score}$  is given in Equation (11), and  $\tau$  is a predefined threshold.

#### Model Categorization

Through the above steps, models fitted from anomaly data blocks are identified. Different underground anomalies introduce unique dynamics in GPR data due to distinct changing

information along and among the collected EM waves. As a result, models from different anomaly types differ significantly, while those from the same anomaly type are similar due to consistent inherent dynamics. This forms a category-discriminative CuCoRes model space, where clustering approaches<sup>5</sup> could be performed to categorize models, with each cluster representing a specific anomaly type.

## 4 Experimental Study

All experiments are conducted using Python 3.6 on a desktop with an Intel Core i5-11500 2.70-GHz CPU, 16-GB RAM, and a GeForce RTX 3080Ti 12G graphics card. For the implementation of our approach, we initialize the input weights and reservoir weights of CuCoRes randomly following a standard normal distribution. The size of each reservoir is default set as 50, the spectral radii are set to 0.9. The anomaly score threshold  $\tau$  is defined as the maximum of the minimum distances between any normal models. As for the clusters, we use the official implementation from <https://scikit-learn.org/>.

### 4.1 The Utilized 3D GPR data

GPR data is collected from cement and asphalt roads using a 3D GPR system with a 16-channel antenna. The data is segmented into  $16 \times 200 \times 200$  blocks, representing a physical area of approximately 2.5m (width)  $\times$  4m (detecting direction)  $\times$  4m (depth). Each block, except for normal ones, contains an anomaly. The number of blocks per type is shown in Table 1. Three main types of subsurface anomalies are identified: cavities, looseness, and cracks. The GPR data also includes pipelines and manhole covers, also crucial to detect. Examples of GPR data blocks are shown in Figure 5.

Normal	Cavity	Looseness	Crack	Pipeline	Manhole
200	192	203	191	201	192

Table 1: Number of normal and anomaly GPR data blocks by type.

### 4.2 Anomaly Detection of GPR Data

For underground diagnosis, the initial focus involves identifying anomalies in newly collected GPR data using only previously acquired normal data free from subsurface anomalies or other objects. We randomly select 100 normal data blocks for initialization. For testing, the remaining 100 normal blocks and 20 blocks from each anomaly type are used.

To our knowledge, apart from supervised methods requiring multi-type labeled GPR data (discussed in Section 2), no existing research tailored for 3D GPR data performs anomaly detection on new data given only limited normal data support. We evaluate our approach against recent baselines that, while not specifically designed for GPR data, are able to utilize solely normal GPR data for anomaly detection in newly collected data, including: 1) Voxel-based anomaly detection

<sup>5</sup>Clustering techniques such as K-Means [Hartigan and Wong, 1979], Agglomerative Clustering [Ackermann *et al.*, 2014], or Fuzzy C-Means [Bezdek *et al.*, 1984] could be applied, support with the introduced model distance measurement.

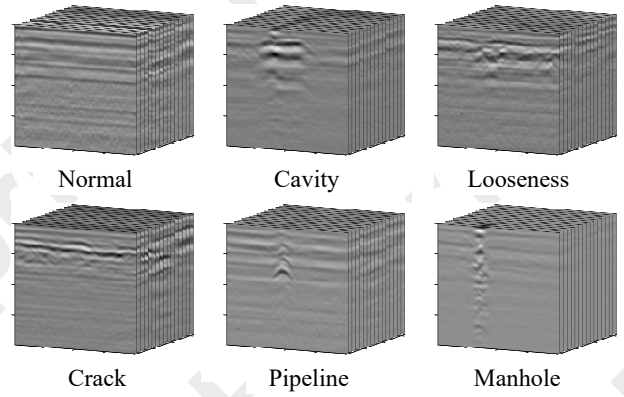


Figure 5: Several examples of 3D GPR data blocks containing different subsurface objects.

Methods	Precision(Pre)	Recall(Rec)	F1-Score
Patchcore-3D	83.2% $\pm$ 2.5%	86.0% $\pm$ 2.1%	84.6% $\pm$ 1.8%
STEAL	84.8% $\pm$ 1.6%	82.7% $\pm$ 2.4%	83.7% $\pm$ 2.0%
3D-VAE	86.0% $\pm$ 2.3%	84.6% $\pm$ 1.1%	85.3% $\pm$ 1.7%
MemAE	79.2% $\pm$ 2.1%	81.6% $\pm$ 2.8%	80.4% $\pm$ 1.4%
f-AnoGAN	81.6% $\pm$ 1.0%	79.8% $\pm$ 2.6%	80.7% $\pm$ 2.2%
SimpleNet	80.9% $\pm$ 1.4%	79.3% $\pm$ 2.3%	79.6% $\pm$ 1.2%
CubeRes (w/o)	87.9% $\pm$ 1.9%	87.3% $\pm$ 2.5%	87.6% $\pm$ 2.0%
CuCoRes (ED.)	90.1% $\pm$ 2.6%	89.2% $\pm$ 1.8%	89.7% $\pm$ 2.0%
<b>Our Approach</b>	<b>92.2% <math>\pm</math> 1.8%</b>	<b>91.7% <math>\pm</math> 1.2%</b>	<b>91.9% <math>\pm</math> 1.4%</b>

Table 2: Anomaly detection using our approach against baselines in terms of Pre, Rec, and F1-Score.

methods, which treats 3D DPR data as a three-dimensional matrix: Patchcore-3D [Frolova *et al.*, 2023], Synthetic Temporal Anomaly Guided End-to-End Video Anomaly Detection (STEAL) [Astrid *et al.*, 2021], 3D-VAE [Brock *et al.*, 2016], MemAE [Gong *et al.*, 2019], and Cube Reservoir Computing without optimization (CubeRes w/o) since only normal data is provided [Zhou *et al.*, 2024]; 2) Image-based anomaly detection approaches, in which 3D DPR data is considered as a multi-channel image: f-AnoGAN [Schlegl *et al.*, 2019], and SimpleNet [Liu *et al.*, 2023];

The results<sup>6</sup> are presented in Table 2. Voxel-based methods like Patchcore-3D, STEAL, etc, treat 3D GPR data as three-dimensional matrices, but struggle with the given insufficient normal data for effective optimization, failing to distinguish variations among normal and abnormal patterns in GPR data. Image-based methods, such as f-AnoGAN and SimpleNet, designed for 2D image format, overlook effective changing information of a certain dimension and fail to adequately capture the internal dynamics in 3D GPR data. Building correlations along and among EM waves, fitting GPR data via CuCoRes adequately and accurately capturing the data-inherent multi-directional dynamics. Consequently, CuCoRes models fitted from anomaly blocks, markedly differ from those derived from normal. Focusing on the data-

<sup>6</sup>CuCoRes (ED.) refers to the result obtained by using the Euclidean distance to measure the difference between CuCoRes models, subsequently discussed in Subsection 4.4: Ablation Study.

inherent changing information, our approach demonstrates superior anomaly detection performance compared to baselines, even with the given minimal normal data support.

### 4.3 The Model/Feature Clustering Results

After identifying abnormal models, our approach employs clustering to categorize these models, grouping data blocks originating from the same type of anomalies. The introduced CuCoRes fits and captures the multi-directional dynamics within the GPR data without offline iterative training. The fitted models serve as representations of the original blocks.

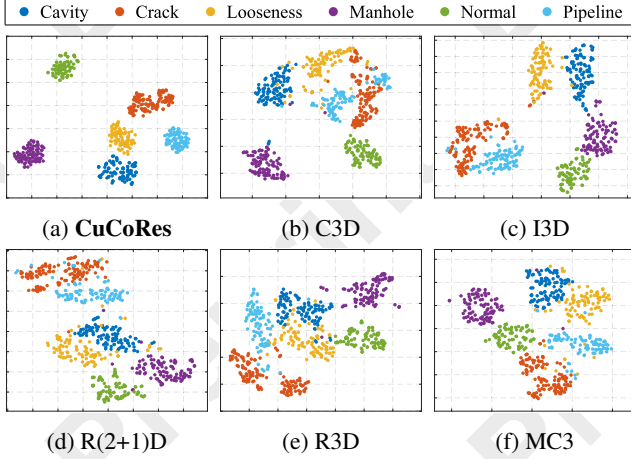


Figure 6: CuCoRes model space demonstrates enhanced category discrimination: 1) Marked separation between normal and abnormal models ensures reliable anomaly detection; 2) Smaller distances within classes and larger distances between classes allow for effective clustering of different anomaly types.

We adopt feature extractors including, 3D ResNet (R3D) [Hara *et al.*, 2017], 3D Convolutional Neural Networks (C3D) [Tran *et al.*, 2015], (2+1)D Convolutional Networks (R(2+1)D) [Tran *et al.*, 2018], Mixed Convolutions 3D and 2D (MC3) and Inflated 3D ConvNet (I3D) [Carreira and Zisserman, 2017] on the identified abnormal blocks<sup>7</sup>. We also utilized CubeRes (w/o) [Zhou *et al.*, 2024] for data fitting and representation. These features/models are clustered by three widely used clustering algorithms: K-Means, Agglomerative clustering (AC), and Fuzzy C-Means (FCM).

Table 3 shows that CuCoRes surpasses other methods in anomaly clustering. Using t-SNE [Van der Maaten and Hinton, 2008], we visualized the fitted models and other features in 2D space (Figure 6), where each point represents a fitted model or feature associated with a GPR data block. Although GPR data appears image-like, it fundamentally represents EM wave collections with unique dynamics arising from variations along and among the waves caused by different underground anomalies. Pre-trained deep neural networks, primarily designed for visual feature extraction, struggle to capture and distinguish these dynamics effectively. CuCoRes, focusing on data-inherent changing information, captures multi-directional dynamics by establishing correlation-

<sup>7</sup>Pre-trained on Kinetics dataset [Carreira and Zisserman, 2017].

Methods	K-Means			AC			FCM		
	Acc	ARI	NMI	Acc	ARI	NMI	Acc	ARI	NMI
C3D	0.57	0.36	0.55	0.69	0.57	0.67	0.64	0.46	0.60
MC3	0.85	0.72	0.76	0.93	0.83	0.85	0.85	0.74	0.77
R(2+1)D	0.76	0.58	0.68	0.81	0.64	0.74	0.60	0.44	0.57
I3D	0.74	0.69	0.79	0.76	0.72	0.83	0.75	0.69	0.78
R3D	0.82	0.62	0.67	0.73	0.61	0.72	0.83	0.65	0.69
CubeRes (w/o)	0.90	0.87	0.86	0.91	0.87	0.88	0.90	0.85	0.87
CuCoRes (w/E)	0.92	0.86	0.85	0.92	0.88	0.88	0.92	0.86	0.87
<b>CuCoRes</b>	<b>0.96</b>	<b>0.91</b>	<b>0.90</b>	<b>0.97</b>	<b>0.93</b>	<b>0.93</b>	<b>0.95</b>	<b>0.89</b>	<b>0.91</b>

Table 3: The models/features clustering results: Accuracy (Acc), Adjusted Rand Index (ARI), and Normalized Mutual Info (NMI).

adjusted connections within the data block across multiple directions. Owing to the distinct dynamics captured, the models derived from CuCoRes exhibit superior clustering performance on different types of subsurface anomalies.

### 4.4 Ablation Study

Our approach incorporates three key attributes: 1) Three reservoirs in CuCoRes’ hidden layer to adequately capture multi-directional dynamics; 2) Spatial correlation adjustments to strengthen correlations with nearby points while reducing those with distant ones, enabling accurate dynamic capture; 3) A direct-solvable model distance measurement to evaluate the difference between CuCoRes models.

For the first attribute, we exclude experiments with the LMS method using ESN (with one reservoir) to fit GPR data blocks [Liu *et al.*, 2024], due to the impractically large size of the ESN readout model, which is  $200 \times 16 \times \text{reservoir size}$  when fitted along the detecting direction, and is not directly classifiable. In contrast, CuCoRes captures multi-directional dynamics more compactly with a fitted model size of  $3 \times \text{reservoir size}$ , enabling efficient learning on the models.

For the second, we perform clustering on CuCoRes models but remove spatial correlation adjustments **E** during fitting, denoted as CuCoRes (w/o **E**) in Table 3, where introducing spatial correlation adjustments improves clustering by about 5%, achieving a more accurate dynamic capture and category-discriminative model space. As for the third, using Euclidean Distance to replace the introduced model distance measurement, as indicated by CuCoRes (ED.) in Table 2, decreases the effectiveness of anomaly detection by about 3%.

## 5 Conclusion

This study proposes learning in the CuCoRes model space for anomaly detection in 3D GPR data: 1) CuCoRes, incorporating three reservoirs and spatial correlation adjustment, effectively captures multi-directional dynamics into compact fitted models; 2) Representing GPR data with fitted models enables anomaly detection in category-discriminative model space, distinguishing anomalies while grouping same-type ones; 3) Our approach relies on limited, easily accessible normal GPR data, enhancing practicality in real-world scenarios. Future work will explore reconstructing anomaly regions for intuitive visualization to aid repairs.



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